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The ATLAS^{3D} project – XV. Benchmark for early-type galaxies scaling relations from 260 dynamical models: mass-to-light ratio, dark matter, Fundamental Plane and Mass Plane

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ABSTRACT

We study the volume-limited and nearly mass-selected (stellar mass $M_{\text{stars}} \gtrsim 6 \times 10^9 M_{\odot}$) ATLAS^{3D} sample of 260 early-type galaxies (ETGs, ellipticals Es and lenticulars S0s). We construct detailed axisymmetric dynamical models (Jeans Anisotropic MGE), which allow for orbital anisotropy, include a dark matter halo and reproduce in detail both the galaxy images and the high-quality integral-field stellar kinematics out to about $1R_e$, the projected half-light radius. We derive accurate total mass-to-light ratios $(M/L)_e$ and dark matter fractions f_{DM} , within a sphere of radius $r = R_e$ centred on the galaxies. We also measure the stellar $(M/L)_{\text{stars}}$ and derive a median dark matter fraction $f_{\text{DM}} = 13$ per cent in our sample. We infer masses $M_{\text{JAM}} \equiv L \times (M/L)_e \approx 2 \times M_{1/2}$, where $M_{1/2}$ is the total mass within a sphere enclosing half of the galaxy light. We find that the thin two-dimensional subset spanned by galaxies in the $(M_{\text{JAM}}, \sigma_e, R_e^{\text{maj}})$ coordinates system, which we call the Mass Plane (MP) has an observed rms scatter of 19 per cent, which implies an intrinsic one of 11 per cent. Here, R_e^{maj} is the major axis of an isophote enclosing half of the *observed* galaxy light, while σ_e is measured

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within that isophote. The MP satisfies the scalar virial relation $M_{\text{JAM}} \propto \sigma_e^2 R_e^{\text{maj}}$ within our tight errors. This shows that the larger scatter in the Fundamental Plane (FP) (L , σ_e , R_e) is due to stellar population effects [including trends in the stellar initial mass function (IMF)]. It confirms that the FP deviation from the virial exponents is due to a genuine $(M/L)_e$ variation. However, the details of how both R_e and σ_e are determined are critical in defining the precise deviation from the virial exponents. The main uncertainty in masses or M/L estimates using the scalar virial relation is in the measurement of R_e . This problem is already relevant for nearby galaxies and may cause significant biases in virial mass and size determinations at high redshift. Dynamical models can eliminate these problems. We revisit the $(M/L)_e - \sigma_e$ relation, which describes most of the deviations between the MP and the FP. The best-fitting relation is $(M/L)_e \propto \sigma_e^{0.72}$ (r band). It provides an upper limit to any systematic increase of the IMF mass normalization with σ_e . The correlation is more shallow and has smaller scatter for slow rotating systems or for galaxies in Virgo. For the latter, when using the best distance estimates, we observe a scatter in $(M/L)_e$ of 11 per cent, and infer an intrinsic one of 8 per cent. We perform an accurate empirical study of the link between σ_e and the galaxies circular velocity V_{circ} within $1R_e$ (where stars dominate) and find the relation $\max(V_{\text{circ}}) \approx 1.76 \times \sigma_e$, which has an observed scatter of 7 per cent. The accurate parameters described in this paper are used in the companion Paper XX (Cappellari et al.) of this series to explore the variation of global galaxy properties, including the IMF, on the projections of the MP.

Key words: galaxies: elliptical and lenticular, cD – galaxies: evolution – galaxies: formation – galaxies: kinematics and dynamics – galaxies: structure.

1 INTRODUCTION

Scaling relations of early-type galaxies (ETGs, ellipticals Es and lenticulars S0s) have played a central role in our understanding of galaxy evolution, since the discovery that the stellar velocity dispersion σ (Minkowski 1962; Faber & Jackson 1976) and the galaxy projected half-light radius R_e (Kormendy 1977) correlate with galaxy luminosity L . An important step forward was made with the discovery that these two relations are just projections of a relatively narrow plane, the Fundamental Plane (FP) (Djorgovski & Davis 1987; Dressler et al. 1987; Faber et al. 1987), relating the three variables (L , σ_e , R_e). When the plane is used as a distance indicator, as was especially the case at the time of its discovery, the luminosity can be replaced by the surface brightness within R_e as $\Sigma_e \equiv L/(2\pi R_e^2)$ and the observed plane assumes the form

$$R_e \propto \sigma^{1.33} \Sigma_e^{-0.82}, \quad (1)$$

where the adopted parameters are the median of the 11 independent determinations tabulated in Bernardi et al. (2003).

It was immediately realized that the existence of the FP could be due to the galaxies being in virial equilibrium (e.g. Binney & Tremaine 2008) and that the deviation (tilt) of the coefficients from the virial predictions $R_e \propto \sigma^2 \Sigma_e^{-1}$, could be explained by a smooth power-law variation of mass-to-light ratio (M/L) with mass (Faber et al. 1987). The FP showed that galaxies assemble via regular processes and that their properties are closely related to their mass. The tightness of the plane gives constraints on the variation of stellar population among galaxies of similar characteristics and on their dark matter content (Renzini & Ciotti 1993; Borriello, Salucci & Danese 2003). The regularity also allows one to use the FP to study galaxy evolution, by tracing its variations with redshift (van Dokkum & Franx 1996).

However, other reasons for the deviation of the coefficients are possible: the constant coefficients in the simple virial relation only rigorously apply if galaxies are spherical and homologous systems, with similar profiles and dark matter fraction. But both galaxies

concentration (Caon, Capaccioli & D’Onofrio 1993) and the amount of random motions in their stars (Davies et al. 1983) were found to systematically increase with galaxy luminosity.

The uncertain origin of the tilt led to a large number of investigations about its origin, exploring the effects of (i) the systematic variation in the stellar population or initial mass function (IMF; e.g. Prugniel & Simien 1996; Forbes, Ponman & Brown 1998) or (ii) the non-homology in the surface brightness distribution (e.g. Graham & Colless 1997; Prugniel & Simien 1997; Bertin, Ciotti & Del Principe 2002; Trujillo, Burkert & Bell 2004) or (iii) the kinematics (e.g. Prugniel & Simien 1994; Busarello et al. 1997) or (iv) the variation in the amount of dark matter (e.g. Renzini & Ciotti 1993; Ciotti, Lanzoni & Renzini 1996; Borriello et al. 2003) on the FP tilt and scatter. Those works were all based on approximate galaxy spherical models, trying to test general hypotheses and not reproducing real galaxies in detail, which sometimes led to contrasting results. What became clear however was that various effects could potentially influence a major part of the FP tilt. Moreover, it was found that the small scatter in the FP implies a well-regulated formation for ETGs.

The next step forward came with subsequent studies, which instead of testing general trends, used small samples of objects and tried to push to the limit the accuracy of measuring galaxy central masses, while reducing biases as much as possible. Those accurate total masses could be directly compared to the simple virial ones, testing for residual trends. Similar but independent studies were performed using two completely different techniques, either stellar dynamics (Cappellari et al. 2006) or strong gravitational lensing (Bolton et al. 2007, 2008; Auger et al. 2010b). The results from those efforts agree with each other’s, and showed that the tilt of the FP is almost entirely due to a genuine M/L variation.

In this paper, we investigate once more the origin of the FP tilt. This new study is motivated by the dramatic increase in the size and quality of our galaxy sample, with respect to any previous similar study. We have in fact state-of-the-art SAURON (Bacon et al. 2001) stellar kinematics for all the 260 ETGs of the ATLAS^{3D}

sample (Cappellari et al. 2011a, hereafter Paper I), which constitute a volume-limited and carefully selected sample of ETGs, down to a stellar mass of about $M_{\text{stars}} \gtrsim 6 \times 10^9 M_{\odot}$. This fact, combined with detailed dynamical models for the entire sample, allows us to test previous claims with unprecedented accuracy. The new models also include a dark matter halo and give constraints on the dark matter content in the centres of ETGs. These measurements will be used in the companion Cappellari et al. (2013, hereafter Paper XX) to provide a novel view of galaxy scaling relations.

In what follows, in Section 2 we present the sample and data, in Section 3 we describe the methods used to extract our quantities, in Section 4 we present our results on the FP tilt, dark matter and the (M/L)– σ relation, and finally, we summarize our paper in Section 5.

2 SAMPLE AND DATA

2.1 Selection

The galaxies studied in this work are the 260 ETGs which constitute the volume-limited and nearly mass-selected ATLAS^{3D} sample (Paper I). The object were morphologically selected as early type according to the classic criterion (Hubble 1936; de Vaucouleurs 1959; Sandage 1961) of not showing spiral arms or a disc-scale dust lane (when seen edge-on). The early types are extracted from a parent sample of 871 galaxies of all morphological types brighter than $M_K = -21.5$ mag, using 2MASS photometry (Skrutskie et al. 2006), inside a local ($D < 42$ Mpc) volume of $1.16 \times 10^5 \text{ Mpc}^3$ (see full details in Paper I).

2.2 Comparison to previous samples: dynamics and lensing

Our goal is to measure total masses, or equivalently M/L, in the central regions of galaxies. M/L of significant samples of individual ETGs have been previously obtained via dynamical modelling (e.g. 37 ETGs, van der Marel 1991; 36 ETGs, Magorrian et al. 1998; 21 ETGs, Gerhard et al. 2001; 25 ETGs, Cappellari et al. 2006; 16 ETGs, Thomas et al. 2007b; 14 ETGs, Williams, Bureau & Cappellari 2009; 48 ETGs, Scott et al. 2009) or strong gravitational lensing (e.g. 22 ETGs, Rusin, Kochanek & Keeton 2003; 15 ETGs, Koopmans et al. 2006; 53 ETGs, Bolton et al. 2008; 73 ETGs, Auger et al. 2010b). An important, and perhaps not obvious, difference between the quantities obtained with the two techniques is that the dynamical models provide masses enclosed within a *spherical* radius, while strong lensing measures the mass inside a *cylinder* with axis parallel to the line of sight (LOS). Care has to be taken when comparing the two methods. An illustration of this fact is given in fig. 1 of Dutton et al. (2011b).

An advantage of the strong lensing technique is that the recovered mass inside a cylinder with the radius of the Einstein ring is nearly insensitive to the mass distribution, and completely independent of the stellar dynamics. However, the requirement of a galaxy to act as a strong lens, necessarily imposes biases in the objects selection, and in particular limits mass measurements via strong lensing to the most massive nearby ETGs ($\sigma \gtrsim 200 \text{ km s}^{-1}$ in Auger et al. 2010b).

The dynamical modelling technique has the significant advantage that it can in principle be applied to any bound system made of stars. However, it requires a detailed treatment of the observed surface brightness and orbital distribution, in combination with integral-field data, for robust and accurate values (e.g. Cappellari et al. 2006).

In this paper, we apply the stellar dynamical modelling technique to the ATLAS^{3D} sample of 260 ETGs. This increases the sample size for which accurate total masses have been measured by a factor of 4. Moreover, the sample is volume limited and statistically representative of the nearby galaxy population with stellar mass $M_{\text{stars}} \gtrsim 6 \times 10^9 M_{\odot}$ and in particular includes ETGs with velocity dispersion as low as $\sigma_e \approx 40 \text{ km s}^{-1}$ (see Paper I for an illustration of the characteristics of the sample).

2.3 Stellar kinematics and imaging

Various multiwavelengths data sets are available for the sample galaxies (see a summary in Paper I). In this work, we make use of the SAURON (Bacon et al. 2001) integral-field stellar kinematics within about one half-light radius R_e , which was introduced in Emsellem et al. (2004), for the subset of 48 early types in the SAURON survey (de Zeeuw et al. 2002), and in Paper I for the rest of the ATLAS^{3D} sample. Maps of the stellar velocity for all the 260 galaxies were presented in Krajnović et al. (2011, hereafter Paper II).

In this paper, we are not interested in the shape of the stellar LOS velocity distribution (LOSVD), but we want to approximate velocity moments which are predicted by the Jeans (1922) equations. In Cappellari et al. (2007), we used semi-analytic models to compute a set of realistic galaxy LOSVDs with known velocity moments, using the Hunter & Qian (1993) formalism, as implemented in Emsellem, Dejonghe & Bacon (1999). The models LOSVDs were used to broaden galaxy spectral templates and noise was subsequently added. The kinematics was then extracted from the synthetic spectra using PPXF (Cappellari & Emsellem 2004) as done for the real galaxies. We found that $V_{\text{rms}} \equiv \sqrt{V^2 + \sigma^2}$, where V and σ are the mean and standard deviation of the best-fitting Gaussian and provide a better empirical approximation to the velocity second moment $\langle v_{\text{los}}^2 \rangle^{1/2}$ than an integral of a more general LOSVD described by the Gauss–Hermite parametrization (Gerhard 1993; van der Marel & Franx 1993). This is due to the large sensitivity of the moments to the wings of the LOSVD, which are observationally ill determined. For this reason, all the kinematic quantities used in the paper are extracted using a simple Gaussian LOSVD in the PPXF software (keyword MOMENTS=2).

The photometry used in this work comes from the Sloan Digital Sky Survey (SDSS; York et al. 2000) data release eight (Aihara et al. 2011) for 225 galaxies and was supplemented by our own photometry taken at the 2.5-m Isaac Newton Telescope (INT) in the same set of filters and with comparable signal to noise for the rest of the sample galaxies (Scott et al. 2013, hereafter Paper XXI).

3 METHODS

3.1 Measuring galaxy enclosed masses

3.1.1 Choosing the dynamical modelling approach

Various dynamical modelling techniques have been developed in the past. They are all characterized by their ability to reproduce in detail, in a *non-parametric* way, the characteristics of the galaxy surface brightness. This contrasts with a more qualitative toy-model approach (e.g. Tortora et al. 2009; Treu et al. 2010) that assumes a spherical shape and a simpler parametrization (e.g. Hernquist 1990 or Sérsic 1968 profile) for the surface brightness of all galaxies. An accurate description of the galaxy surface brightness is a necessary requirement for quantitative and unbiased measurements of

dynamical quantities as much of the kinematic information on real galaxies is contained in the photometry alone (Cappellari 2008). The state of the art in the field is currently represented by Schwarzschild (1979) orbit-superposition approach, which was originally developed to reproduce galaxy stellar densities and was later generalized to produce detailed fits to the stellar kinematics (Richstone & Tremaine 1988; Rix et al. 1997; van der Marel et al. 1998) and has been widely used for determinations of masses of supermassive black holes (e.g. van der Marel et al. 1997; Gebhardt et al. 2000a; Cappellari et al. 2002; Valluri, Merritt & Emsellem 2004; Houghton et al. 2006), for galaxy mass determinations (e.g. Cappellari et al. 2006; Thomas et al. 2007b) and to recover orbital distributions (e.g. Krajnović et al. 2005; Cappellari et al. 2007; van den Bosch et al. 2008; Thomas et al. 2009). A close contender technique, but not as widely used, is the particle-based made-to-measure method of Syer & Tremaine (1996) as implemented to reproduce kinematical observables by various groups (de Lorenzi et al. 2007; Dehnen 2009; Long & Mao 2010). When the gravitational potential is assumed to be known, and the particles are chosen to fully sample all integrals of motion, the method effectively corresponds to a particle-based analogue of Schwarzschild's method, and is expected to provide similar results. However, the method may be very useful when the potential is derived from the particles in a self-consistent way. Not much however is known about the convergence and uniqueness of the solution in this case.

The sophistication and generality of the dynamical models has reached a level that exceeds the amount of information that the observations of external galaxies can provide. As a result the observations are unable to uniquely constrain all the model parameters, which suffer from degeneracies (Dejonghe & Merritt 1992; Gerhard et al. 1998; de Lorenzi et al. 2009; Morganti & Gerhard 2012). A key degeneracy is in the deprojection of the observed surface brightness into a three-dimensional stellar mass distribution, which has been proved to be of mathematical nature (Rybicki 1987; Gerhard & Binney 1996) and applies even when the galaxy is assumed to be axisymmetric. However, similar degeneracies are likely to exist when higher (than zero) moments of the velocity are considered. This is expected from dimensional arguments: the current data provide at most a three-dimensional observable (an integral-field data cube), which is the minimum requirement to constrain the orbital distribution, which depends on three integrals of motion, for an assumed potential and known light distribution. It is unlikely for the data to contain enough information to constrain additional parameters, like the dark matter halo shape and the viewing angles (e.g. Valluri et al. 2004). Numerical experiments confirm that even with the best-available integral-field stellar kinematics, and assuming that the gravitational potential is known and axisymmetric, not even the galaxy inclination can be inferred from the data using general Schwarzschild's models (Krajnović et al. 2005; Cappellari et al. 2006; van den Bosch & van de Ven 2009). This implies that the mass distribution is also quite poorly known.

The situation becomes even more problematic when one considers the fact that the majority of ETGs are likely to have bars. 30 percent have obvious bars (Paper II) in the ATLAS^{3D} sample, but more must be hidden by projection effects. Bars are characterized by figure rotation which is ignored by most popular modelling approaches. The treatment of bars could be included in the models as demonstrated in the two-dimensional limit by Pfenniger (1984) and as done to model the Milky Way in three dimension (Zhao 1996; Häfner et al. 2000; Bissantz, Debattista & Gerhard 2004). However, no applications to external galaxies exist. This is due to the extra degeneracy that the addition of at least two extra model

parameters, the bar pattern speed and position angle, will produce on an already degenerate problem. This combines with the dramatic increase in the non-uniqueness of the mass deprojection expected in a triaxial rather than axisymmetric distribution (Gerhard 1996) and with the additional unavoidable biases introduced by observational errors. All this is expected to further broaden the minima in the χ^2 distributions of the fits and to increase the uncertainties and covariances in the recovered parameters.

We chose a different approach. Rather than allowing for the full generality and degeneracies of the models, we adopt a modelling method that makes empirically motivated assumptions to restrict the range of model solutions and improve the accuracy of the mass recovery. This is motivated by the finding that the kinematics of real fast-rotator ETGs in the SAURON sample (de Zeeuw et al. 2002) is well approximated by models characterized by a remarkably simple and homogeneous dynamics, characterized by a cylindrically aligned and nearly oblate velocity ellipsoid $\sigma_\phi \approx \sigma_R \gtrsim \sigma_z$ (Cappellari 2008), as previously suggested by more general Schwarzschild's models (Cappellari et al. 2007; Thomas et al. 2009). The models are called Jeans Anisotropic MGE (JAM), where MGE stands for the Multi-Gaussian Expansion method of Emsellem, Monnet & Bacon (1994), that is used to accurately describe the galaxy photometry. The JAM models can reproduce the full richness of the observed state-of-the-art SAURON integral-field kinematics of fast-rotator ETGs using just two free parameters (Cappellari 2008; Scott et al. 2009; Cappellari et al. 2012), providing a compact description of their dynamics. The JAM models are ideal for this work given that the nearly axisymmetric fast-rotator ETGs constitute the 86 per cent of the ATLAS^{3D} sample (Paper II; Emsellem et al. 2011, hereafter Paper III). Moreover, the JAM models only require the first two velocity moments (V and σ), and not the full LOSVD, which is not available for about half of the sample (see Paper I). The JAM models do not have the freedom to actually fit small-scale details of the kinematics, but they make a prediction based on an accurate description of the photometry and a couple of parameters. This constitutes an advantage in presence of noise and systematics in the data, as it makes spurious features easy to recognize and automatically exclude from the fit. Moreover, the approach is at least three orders of magnitudes faster than Schwarzschild's approach.

However, not all ETGs are well described by the JAM models. In fact, some of the slow rotators in ATLAS^{3D} are likely nearly spherical in the region where we have stellar kinematics, but about 10 per cent of the sample galaxies are weakly triaxial or out of equilibrium (Paper II). For those objects, the modelling results should be treated with caution. Errors of up to 20 per cent can arise when measuring masses of triaxial objects with axisymmetric models (Thomas et al. 2007a; van den Bosch & van de Ven 2009) and this should be kept in mind when interpreting our results. However, preliminary tests using real galaxies in the SAURON sample indicate excellent agreement between the M/L recovery using axisymmetric models and triaxial ones with identical data (van den Bosch 2008). Moreover, in what follows, unless explicitly mentioned, we verified that all conclusions are unchanged if we remove the slow-rotator galaxies from the sample. Barred galaxies provide a further complication, which will be discussed in the next section.

3.1.2 JAM models with dark halo

In practice, the modelling approach we use in this paper starts by approximating the observed SDSS and INT r -band surface brightness distribution of the ATLAS^{3D} galaxies using the MGE

parametrization (Emsellem et al. 1994), with the fitting method and MGE_FIT_SECTORS software package¹ of Cappellari (2002). The choice of the photometric band is a compromise between the need of using the reddest band, to reduce the contamination by dust, and the optimal signal to noise in the images. For barred galaxies, the Gaussians of the MGE models are constrained to have the flattening of the outer disc, following Scott et al. (2009, their fig. 4). Full details of the fitting approach and illustrations of the quality of the resulting MGE fits are given in Paper XXI. The MGE models are used as input for the JAM method¹ (Cappellari 2008) which calculates a prediction of the LOS second velocity moments $\langle v_{\text{los}}^2 \rangle^{1/2}$ for given model parameters and compare this to the observed V_{rms} .

In Cappellari et al. (2006), it was shown that, when the surface brightness distribution is accurately reproduced and good quality integral-field data are available, simple two-integral Jeans models measure masses nearly as accurate as those of Schwarzschild’s models, with errors of 6 per cent. The agreement can be further improved by allowing for orbital anisotropy, in which case the two methods give equally accurate results (Cappellari 2008). We have run an extensive set of tests using JAM to determine the M/L of realistic numerical simulations (Lablanche et al. 2012, hereafter Paper XII). We found that for unbarred galaxies, even when the anisotropy is not accurately constant inside the region with kinematic data, the M/L can be recovered with maximum biases as small as 1.5 per cent. The situation changes when the galaxies are barred. In this case, biases of up to 15 per cent can be expected for the typical bar strengths we find in ETGs.

The models we use here were already presented in Cappellari et al. (2012), where they were used to uncover a systematic variation of the stellar IMF in ETGs. That paper (their table 1) describes six sets of JAM models for all the ATLAS^{3D} galaxies, making various assumptions on the dark matter halo. Given that the SAURON data are typically spatially limited to $1R_e$, one cannot expect to be able to robustly characterize the shape of the dark halo out to large radii from them (Mamon & Łokas 2005). However, as long as the density distribution of the halo is not the same as the one of the stars, we can determine how much room the models allow for a dark matter halo, within the region constrained by the kinematics. The models were summarized in Cappellari et al. (2012), but we describe them here in some more detail using the same lettering notation as that paper:

(A) *Self-consistent JAM model*. Here, we assume that the mass distribution follows the light one as inferred from the deprojected MGE. In this case, the model has three free parameters. Two parameters are non-linear: (i) the vertical anisotropy $\beta_z = 1 - \sigma_z^2/\sigma_R^2$ and (ii) the galaxy inclination i , which together uniquely specify the shape of the second velocity moment $\langle v_{\text{los}}^2 \rangle$, which is then linearly scaled by the $(M/L)_{\text{JAM}}$ to fit the two-dimensional V_{rms} data. We emphasize that, even though the models do not include a dark halo explicitly, $(M/L)_{\text{JAM}}$ does *not* represent the stellar M/L, as sometimes incorrectly assumed, but the *total* one, within a spherical region which has the projected size of our data (see discussion in Section 4.1.2). This set of models, like all others, has a central supermassive black hole with mass predicted by the $M_{\text{BH}}-\sigma$ correlation (Ferrarese & Merritt 2000; Gebhardt et al. 2000b), or a black holes mass as published, when available. The supermassive black hole has a minimal effect on M/L in nearly all cases, but we still exclude the central $R < 2$ arcsec from the fits, for maximum robustness. All our best fitting mass-follows-light JAM models are

shown in Fig. 1. The inclination and $(M/L)_{\text{JAM}}$ of the best-fitting models are given in Table 1.

(B) *JAM with NFW dark halo*. This set of models adopts the approach introduced by Rix et al. (1997) to reduce the halo to a one-parameter family of models. This approach was already used with axisymmetric JAM models of disc galaxies, as done here, by Williams et al. (2009) and to construct spherical toy models of various stellar systems (Napolitano et al. 2005; Tollerud et al. 2011). We assume the halo is spherical and characterized by the two-parameters double power-law NFW profile (Navarro, Frenk & White 1996). We then adopt the halo mass–concentration $M_{200}-c_{200}$ relation (Navarro et al. 1996) as given by Klypin, Trujillo-Gomez & Primack (2011) to make the halo profile a unique function of its mass M_{200} . The latter is not a critical assumption: our observations only sample a region well inside the predicted halo break radius, so that all our conclusion are unchanged if we describe the halo with a simple power-law density profile $\rho(r) \propto r^{-1}$, as we numerically verified. The resulting JAM models have in this case four parameters: (i) the galaxy inclination i , (ii) the anisotropy β_z , (iii) the *stellar* $(M/L)_{\text{stars}}$, assumed spatially constant and (iv) the halo virial mass M_{200} , defined as the mass within the spherical radius r_{200} at which the average density is equal to 200 times the critical density of the Universe. The $(M/L)_{\text{stars}}$ and dark matter fraction $f_{\text{DM}}(r = R_e)$ of the best-fitting models are given in table 1 of Paper XX.

(C) *JAM with contracted NFW dark halo*. These models include a halo which is originally assumed to be of NFW form, with concentration specified by its mass via the $M_{200}-c_{200}$ relation as in (B). However, during the fitting process, for every choice of the model parameters, the halo is contracted according to the enclosed stellar mass distribution, which is defined by the (circularized) MGE and the corresponding $(M/L)_{\text{stars}}$ parameter. For the contraction, we used the prescription of Gnedin et al. (2011), which is an update of Gnedin et al. (2004). We verified that our IDL code produces the same output as the C language software CONTRA by Gnedin et al. (2004), when the same input is given. The resulting JAM model has the same four free parameters (i , β_z , $(M/L)_{\text{stars}}$, M_{200}) as in (B).

(D) *JAM with general dark halo (gNFW)*. These models include a dark halo that generalizes the NFW profile (see also Barnabè et al. 2012), with density:

$$\rho_{\text{DM}}(r) = \rho_s \left(\frac{r}{r_s} \right)^{\gamma} \left(\frac{1}{2} + \frac{1}{2} \frac{r}{r_s} \right)^{-\gamma-3}. \quad (2)$$

The density has the same large-radii asymptotic power-law slope $\beta = -3$ as the NFW halo, but it allows for a variable inner slope, which we constrained to the bounds $-1.6 < \gamma < 0$, by assigning zero probability to the prior $P(\text{model}) = 0$ (Section 3.1.3) outside this parameters range. The ranges include a flat inner core $\gamma = 0$ and the NFW $\gamma = -1$ as special cases. The upper bound was chosen as the nearly maximum slope we measured for all contracted haloes in (C) (top panel of Fig. 2). However, recent simulations suggest that baryonic effects produce flatter haloes than these predictions for a broad range of galaxy masses (Duffy et al. 2010; Governato et al. 2010; Inoue & Saitoh 2011; Laporte et al. 2012; Macciò et al. 2012; Martizzi et al. 2012; Pontzen & Governato 2012). Note that our adopted maximum halo slope is still generally more shallow than the typical ‘isothermal’ average power slope $\gamma' = 2.0$ that we measure for the stellar density alone within $1R_e$ (bottom panel of Fig. 2). This fact is important to avoid model degeneracies between the stellar and halo densities. This model is the most general of all six and it includes any of the other five models as special cases. It has five free parameters: (i) the galaxy inclination, (ii) the anisotropy β_z , (iii) the stellar mass M_{stars} , (iv) the halo inner slope γ and (v) the

¹ Available from <http://purl.org/cappellari/idl>

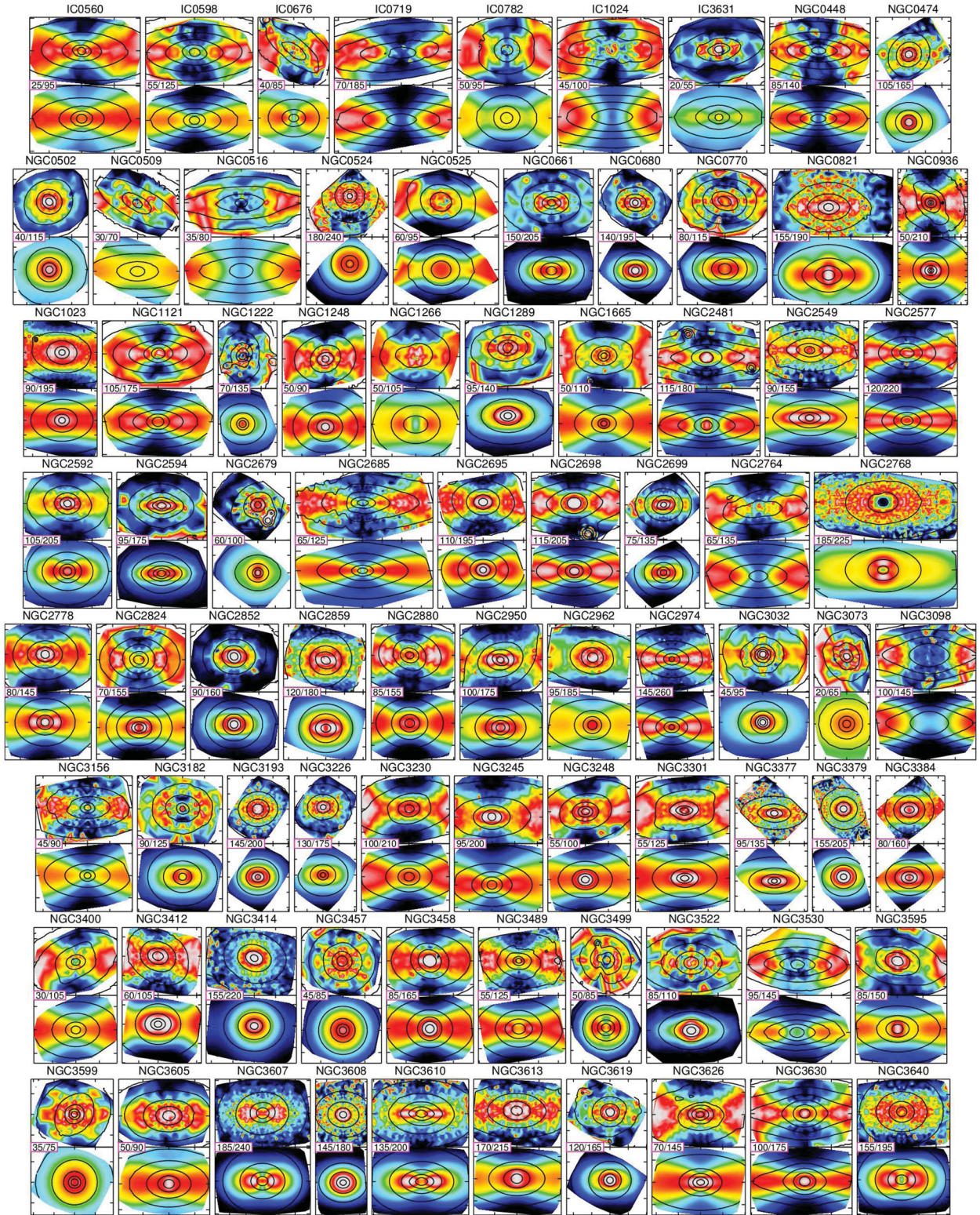


Figure 1. Mass-follows-light JAM models of the ATLAS^{3D} sample. In each panel, the top plot shows the by-symmetrized and linearly interpolated SAURON $V_{\text{rms}} \equiv \sqrt{V^2 + \sigma^2}$, where V is the mean stellar velocity and σ is the stellar velocity dispersion. V_{rms} ranges are printed. Ticks are separated by 10 arcsec. The observed galaxy surface brightness is overlaid, in steps of 1 mag. The bottom plot shows the best-fitting JAM model, and the adopted MGE surface brightness. These models (A) have just two free non-linear parameters, the inclination and the global anisotropy (i , β_z), to reproduce the shape of the observed V_{rms} . Yet, once the surface brightness is given, most of the variety in our maps can be reproduced. Nearly all significant deviations between data and models are due to bars, recognizable from the asymmetries in the observed surface brightness, dust, which affects both the mass model and the kinematics, or inferior data. The predictive power of these simple JAM models qualitatively suggests that the assumed total potential is not significantly in error, which implies that dark matter is unimportant (or accurately follows the light). The good fits also show that ETGs have a simple dynamics within $1R_e$.

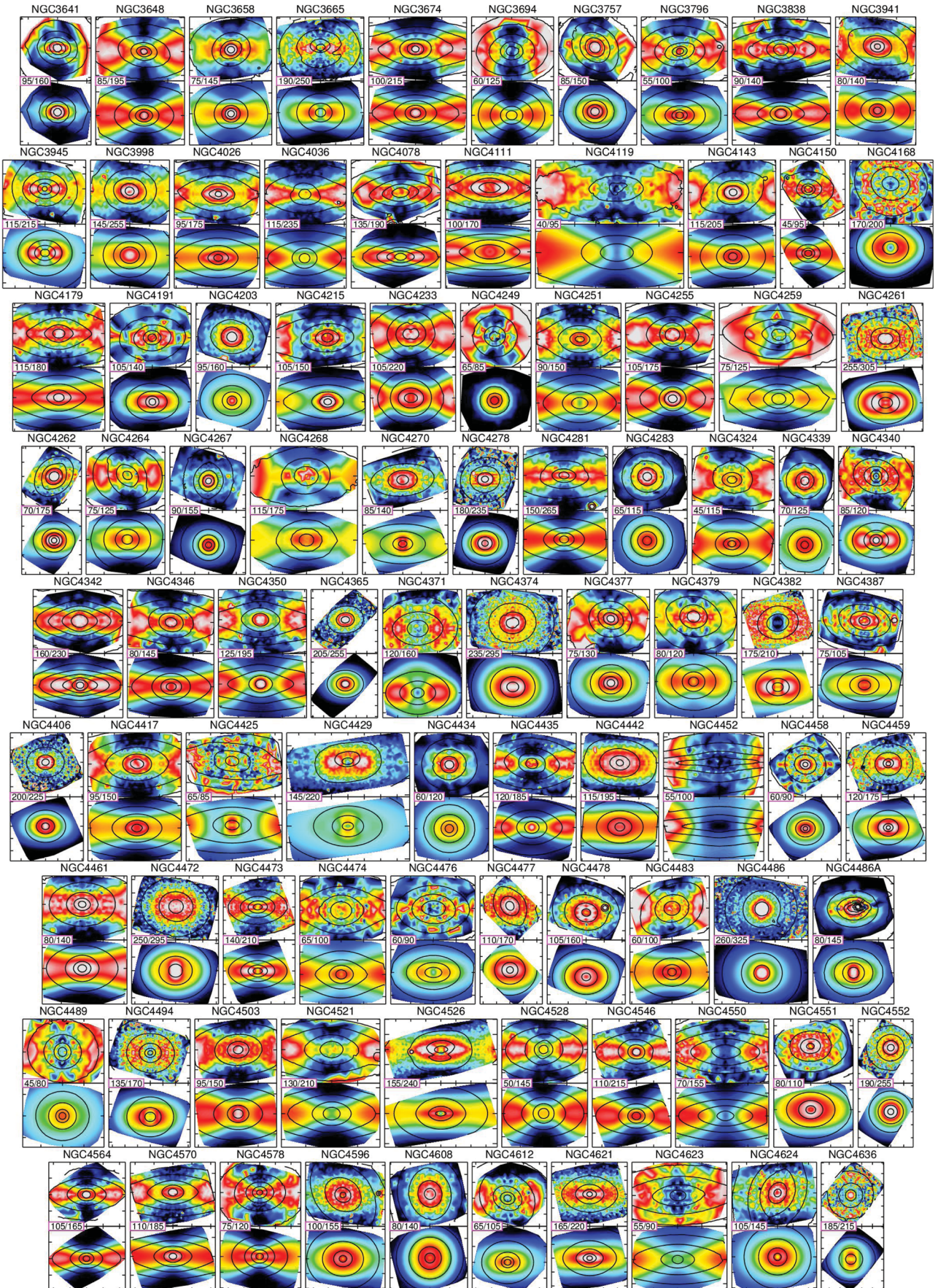


Figure 1 – continued

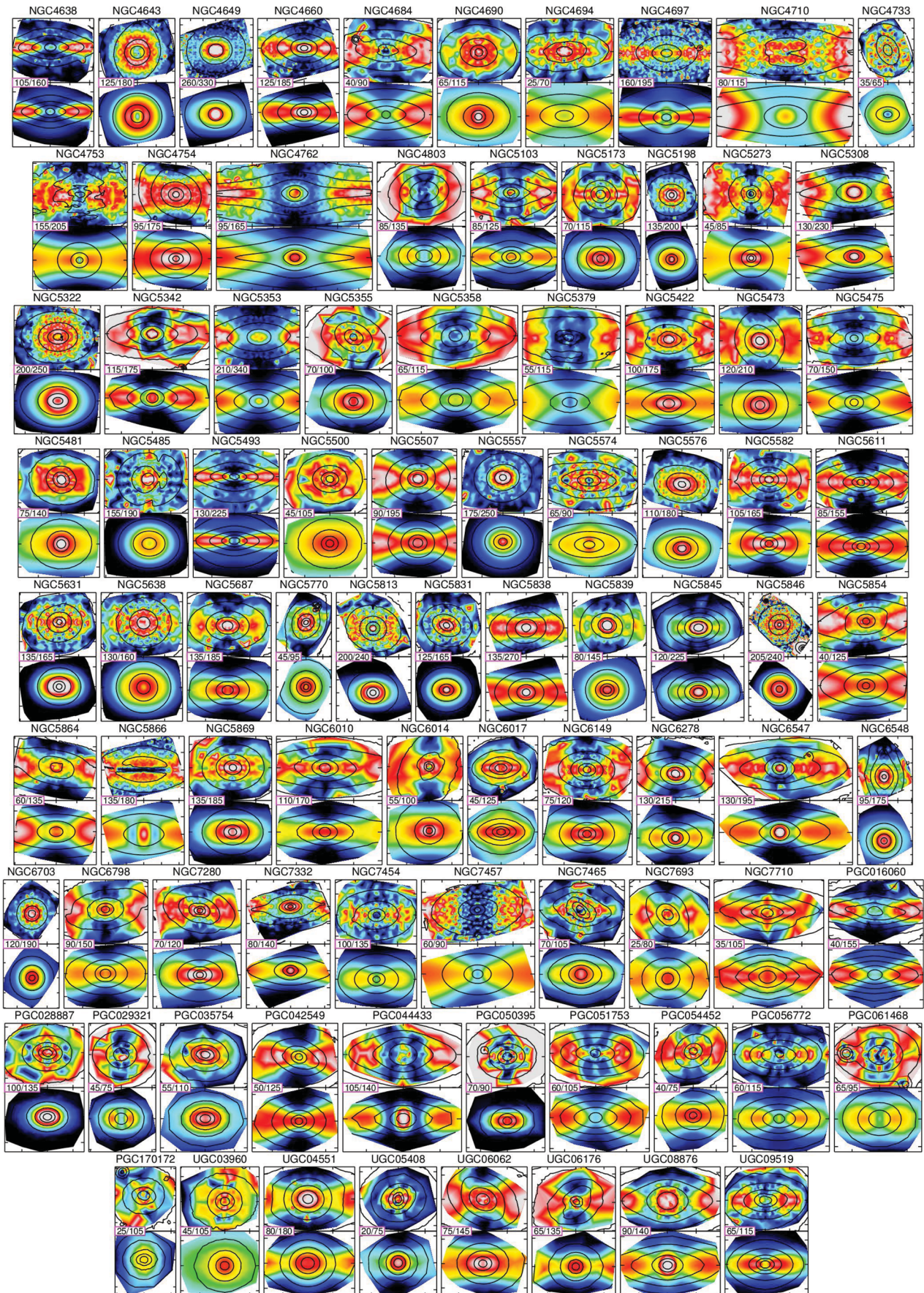


Figure 1 – continued

Table 1. Scaling relations and mass-follows-light JAM models parameters for the ATLAS^{3D} sample of 260 ETGs (see Supporting Information).

Galaxy	$\log \sigma_e$ (km s^{-1})	$R(\sigma)/R_e$	$\log \sigma_{\text{kpc}}$ (km s^{-1})	Inc ($^\circ$)	$\log(M/L)_{\text{JAM}}$ (M_\odot/L_\odot)	$\log V_{\text{circ}}^{\text{max}}$ (km s^{-1})	qual	$\log R_e^{\text{maj}}$ (arcsec)	$\log R_e$ (arcsec)	$\log r_{1/2}$ (arcsec)	$\log r_g$ (arcsec)	conc	ε_e	$\log L$ (L_\odot)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
IC0560	1.879	0.97	1.885	73	0.486	2.114	2	1.352	1.154	1.248	1.659	0.458	0.577	9.566
IC0598	1.996	1.00	1.964	75	0.439	2.215	2	1.148	0.956	1.109	1.551	0.397	0.567	9.828
IC0676	1.806	0.81	1.825	49	0.550	2.059	0	1.460	1.396	1.477	1.989	0.366	0.259	9.660
IC0719	2.108	0.98	2.019	77	0.938	2.341	3	1.301	1.027	1.155	1.663	0.268	0.716	9.697
IC0782	1.870	1.00	1.827	67	0.670	2.086	1	1.303	1.207	1.339	1.853	0.361	0.301	9.645
IC1024	1.892	0.99	1.825	88	0.696	2.133	2	1.332	1.078	1.276	1.807	0.236	0.687	9.471
IC3631	1.551	1.00	1.647	70	-0.155	1.833	0	1.235	1.062	1.188	1.635	0.388	0.535	9.742
NGC 0448	2.047	1.00	2.021	90	0.523	2.276	2	1.235	1.002	1.203	1.664	0.375	0.656	9.919
NGC 0474	2.160	0.69	2.205	51	0.618	2.418	1	1.511	1.472	1.608	2.003	0.519	0.163	10.314
NGC 0502	1.989	1.00	2.058	20	0.465	2.251	1	1.171	1.160	1.191	1.651	0.475	0.041	9.952
NGC 0509	1.852	0.92	1.846	90	0.530	1.958	0	1.393	1.168	1.373	1.931	0.314	0.633	9.512
NGC 0516	1.843	0.95	1.766	89	0.528	2.006	2	1.408	1.142	1.328	1.862	0.287	0.691	9.609
NGC 0524	2.343	0.79	2.370	20	0.857	2.598	0	1.572	1.564	1.613	2.119	0.377	0.038	10.544
NGC 0525	1.902	1.00	1.949	70	0.711	2.158	1	1.088	1.029	1.117	1.593	0.347	0.210	9.457
NGC 0661	2.251	1.00	2.272	87	0.958	2.489	1	1.284	1.210	1.369	1.805	0.457	0.294	9.974
NGC 0680	2.262	0.99	2.292	86	0.750	2.508	1	1.284	1.239	1.401	1.813	0.487	0.178	10.276
NGC 0770	2.038	0.99	2.048	88	0.516	2.248	0	0.921	0.857	1.004	1.503	0.320	0.260	9.767
NGC 0821	2.254	0.69	2.285	75	0.822	2.484	2	1.641	1.541	1.703	2.117	0.471	0.369	10.273
NGC 0936	2.225	1.00	2.288	37	0.719	2.576	2	1.749	1.724	1.516	1.989	0.490	0.090	10.594
NGC 1023	2.222	0.74	2.262	74	0.532	2.479	3	1.666	1.546	1.639	2.130	0.436	0.398	10.287
NGC 1121	2.225	1.00	2.204	82	0.824	2.435	2	1.000	0.814	0.997	1.415	0.408	0.530	9.737
NGC 1222	1.958	0.97	1.900	50	0.700	2.305	0	1.218	1.188	1.303	1.743	0.451	0.120	9.804
NGC 1248	1.906	1.00	1.923	42	0.324	2.168	2	1.191	1.148	1.026	1.535	0.405	0.178	9.894
NGC 1266	1.898	0.98	1.917	51	0.597	2.163	0	1.330	1.280	1.376	1.921	0.319	0.214	9.814
NGC 1289	2.095	0.98	2.130	89	0.634	2.382	1	1.339	1.233	1.407	1.777	0.495	0.384	10.083
NGC 1665	1.958	0.94	1.996	59	0.498	2.220	1	1.526	1.400	1.445	1.888	0.414	0.431	10.102
NGC 2481	2.224	1.00	2.200	81	0.698	2.422	2	1.186	0.962	1.146	1.579	0.367	0.567	9.999
NGC 2549	2.152	0.94	2.149	89	0.782	2.381	3	1.466	1.280	1.475	1.859	0.456	0.539	9.653
NGC 2577	2.293	0.97	2.293	70	0.874	2.470	3	1.347	1.197	1.242	1.713	0.426	0.467	10.047
NGC 2592	2.282	1.00	2.291	48	0.882	2.504	1	1.148	1.086	1.182	1.573	0.482	0.241	9.796
NGC 2594	2.224	0.99	2.229	90	0.731	2.412	1	0.999	0.856	1.011	1.412	0.501	0.461	9.736
NGC 2679	2.005	0.85	1.986	90	0.486	2.183	0	1.448	1.389	1.537	1.953	0.452	0.234	9.914
NGC 2685	2.019	0.99	1.991	76	0.455	2.212	3	1.572	1.344	1.488	1.928	0.432	0.628	9.857
NGC 2695	2.257	0.99	2.292	47	0.736	2.509	2	1.312	1.237	1.235	1.690	0.465	0.283	10.199
NGC 2698	2.285	0.99	2.280	73	0.749	2.528	3	1.278	1.092	1.227	1.646	0.454	0.503	10.075
NGC 2699	2.104	1.00	2.118	36	0.568	2.350	1	1.078	1.046	1.099	1.548	0.418	0.147	9.819
NGC 2764	2.029	0.98	1.948	69	0.648	2.247	2	1.365	1.171	1.267	1.767	0.290	0.594	9.989
NGC 2768	2.297	0.45	2.313	90	0.933	2.523	1	1.948	1.778	1.976	2.434	0.402	0.526	10.601
NGC 2778	2.121	1.00	2.141	41	0.855	2.395	2	1.236	1.185	1.169	1.573	0.451	0.216	9.642
NGC 2824	2.105	1.00	2.109	53	0.628	2.443	0	0.953	0.904	0.977	1.410	0.485	0.211	9.889
NGC 2852	2.196	1.00	2.203	39	0.835	2.461	1	0.931	0.901	0.977	1.410	0.488	0.118	9.622
NGC 2859	2.212	0.77	2.247	59	0.568	2.485	2	1.463	1.441	1.578	1.965	0.517	0.104	10.404
NGC 2880	2.121	0.92	2.124	51	0.680	2.378	1	1.389	1.312	1.346	1.816	0.453	0.259	9.936
NGC 2950	2.193	1.00	2.198	58	0.588	2.450	1	1.306	1.237	1.361	1.756	0.501	0.265	9.887
NGC 2962	2.162	0.68	2.233	74	0.814	2.442	1	1.591	1.463	1.611	2.054	0.445	0.434	10.284
NGC 2974	2.355	0.88	2.364	57	0.981	2.567	3	1.547	1.441	1.424	1.893	0.443	0.391	10.152
NGC 3032	1.914	0.96	1.963	38	0.310	2.307	0	1.316	1.282	1.363	1.603	0.587	0.147	9.687
NGC 3073	1.794	0.93	1.750	80	0.249	1.937	0	1.325	1.304	1.451	1.897	0.437	0.090	9.701
NGC 3098	2.101	0.98	2.055	90	0.677	2.322	0	1.351	1.013	1.218	1.669	0.294	0.703	9.815
NGC 3156	1.837	0.95	1.831	68	0.382	2.074	1	1.403	1.257	1.384	1.850	0.360	0.491	9.690
NGC 3182	2.052	0.89	2.049	80	0.589	2.255	0	1.390	1.350	1.493	1.954	0.409	0.170	10.100
NGC 3193	2.252	0.73	2.292	83	0.558	2.488	2	1.463	1.439	1.582	1.993	0.465	0.117	10.595
NGC 3226	2.183	0.57	2.223	57	0.873	2.402	2	1.601	1.566	1.697	2.161	0.420	0.153	10.120
NGC 3230	2.256	0.96	2.292	69	0.767	2.484	2	1.368	1.224	1.324	1.757	0.407	0.453	10.345
NGC 3245	2.248	0.80	2.257	64	0.637	2.461	3	1.505	1.367	1.491	1.881	0.476	0.461	10.173
NGC 3248	1.944	0.95	1.973	59	0.474	2.239	2	1.394	1.289	1.364	1.789	0.486	0.371	9.805
NGC 3301	2.045	0.96	2.068	76	0.402	2.339	3	1.411	1.270	1.415	1.775	0.442	0.449	10.078
NGC 3377	2.108	0.52	2.129	89	0.580	2.327	1	1.734	1.591	1.766	2.163	0.474	0.487	9.888
NGC 3379	2.269	0.60	2.294	88	0.706	2.519	3	1.705	1.673	1.820	2.221	0.487	0.130	10.209
NGC 3384	2.140	0.55	2.161	62	0.473	2.412	3	1.643	1.563	1.575	1.970	0.531	0.294	10.091
NGC 3400	1.888	1.00	1.883	58	0.619	2.116	2	1.250	1.163	1.188	1.675	0.362	0.319	9.512
NGC 3412	1.967	0.66	1.984	58	0.404	2.274	1	1.560	1.475	1.516	1.899	0.497	0.254	9.758

Table 1 – *continued*

Galaxy	$\log \sigma_e$ (km s ⁻¹)	$R(\sigma)/R_e$	$\log \sigma_{\text{kpc}}$ (km s ⁻¹)	Inc (°)	$\log(M/L)_{\text{JAM}}$ (M _⊙ /L _⊙)	$\log V_{\text{circ}}^{\text{max}}$ (km s ⁻¹)	qual	$\log R_e^{\text{maj}}$ (arcsec)	$\log R_e$ (arcsec)	$\log r_{1/2}$ (arcsec)	$\log r_g$ (arcsec)	conc	ε_e	$\log L$ (L _⊙)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
NGC 3414	2.277	0.63	2.327	87	0.779	2.513	1	1.558	1.484	1.642	2.042	0.459	0.226	10.326
NGC 3457	1.861	1.00	1.867	64	0.307	2.122	0	1.068	1.067	1.203	1.598	0.444	0.010	9.534
NGC 3458	2.182	1.00	2.193	52	0.664	2.470	2	0.991	0.973	1.073	1.469	0.463	0.064	9.952
NGC 3489	2.005	0.86	2.009	61	0.260	2.256	2	1.430	1.353	1.378	1.828	0.431	0.273	9.927
NGC 3499	1.856	1.00	1.857	26	0.425	2.204	0	0.907	0.891	0.977	1.320	0.370	0.081	9.489
NGC 3522	1.993	1.00	1.997	89	0.705	2.271	0	1.278	1.147	1.324	1.718	0.470	0.430	9.600
NGC 3530	2.068	1.00	2.052	90	0.718	2.281	0	1.013	0.777	0.974	1.422	0.341	0.628	9.573
NGC 3595	2.129	0.99	2.163	66	0.602	2.355	1	1.287	1.155	1.248	1.688	0.448	0.431	10.064
NGC 3599	1.804	0.73	1.860	26	0.263	2.117	0	1.450	1.449	1.560	1.949	0.475	0.004	9.732
NGC 3605	1.923	1.00	1.932	63	0.460	2.142	1	1.225	1.113	1.220	1.677	0.415	0.394	9.542
NGC 3607	2.315	0.61	2.360	46	0.681	2.580	2	1.693	1.658	1.773	2.175	0.460	0.161	10.661
NGC 3608	2.228	0.68	2.253	88	0.710	2.457	0	1.528	1.472	1.631	2.039	0.462	0.221	10.246
NGC 3610	2.260	1.00	2.266	90	0.496	2.484	3	1.335	1.230	1.397	1.786	0.497	0.391	10.248
NGC 3613	2.294	0.77	2.318	89	0.772	2.523	2	1.554	1.394	1.575	2.021	0.416	0.496	10.456
NGC 3619	2.157	0.63	2.195	42	0.693	2.446	1	1.527	1.504	1.631	2.001	0.509	0.106	10.212
NGC 3626	2.118	0.81	2.119	66	0.437	2.394	1	1.542	1.391	1.513	1.867	0.513	0.495	10.102
NGC 3630	2.195	1.00	2.185	83	0.663	2.443	3	1.233	1.022	1.207	1.607	0.403	0.485	9.957
NGC 3640	2.246	0.69	2.263	68	0.603	2.474	2	1.627	1.585	1.728	2.183	0.432	0.188	10.620
NGC 3641	2.150	1.00	2.165	26	0.949	2.493	0	1.086	1.067	0.937	1.405	0.561	0.084	9.543
NGC 3648	2.224	1.00	2.218	57	0.829	2.475	2	1.195	1.085	1.072	1.494	0.474	0.378	9.910
NGC 3658	2.101	0.93	2.169	42	0.573	2.427	3	1.378	1.326	1.232	1.652	0.538	0.199	10.109
NGC 3665	2.335	0.63	2.354	51	0.796	2.568	2	1.692	1.640	1.750	2.207	0.425	0.218	10.760
NGC 3674	2.268	1.00	2.273	76	0.843	2.504	2	1.126	0.973	1.105	1.529	0.400	0.443	9.984
NGC 3694	1.941	1.00	1.930	42	0.565	2.273	0	1.045	0.984	0.903	1.381	0.361	0.245	9.750
NGC 3757	2.128	1.00	2.121	50	0.673	2.397	0	0.918	0.897	1.022	1.459	0.414	0.103	9.631
NGC 3796	1.916	1.00	1.914	68	0.460	2.185	0	1.151	1.051	1.195	1.602	0.469	0.371	9.527
NGC 3838	2.125	1.00	2.113	79	0.589	2.363	2	1.195	0.974	1.150	1.551	0.423	0.553	9.772
NGC 3941	2.081	0.82	2.089	57	0.400	2.322	1	1.502	1.396	1.487	1.878	0.453	0.378	9.940
NGC 3945	2.249	0.90	2.289	46	0.628	2.534	1	1.506	1.473	1.587	1.954	0.487	0.165	10.394
NGC 3998	2.350	0.82	2.360	38	0.971	2.638	2	1.421	1.380	1.352	1.806	0.472	0.174	9.967
NGC 4026	2.195	0.89	2.199	84	0.675	2.433	2	1.483	1.291	1.464	1.865	0.418	0.535	9.906
NGC 4036	2.260	0.78	2.258	75	0.698	2.478	2	1.619	1.410	1.498	1.954	0.366	0.589	10.463
NGC 4078	2.264	1.00	2.250	90	0.876	2.453	1	1.169	0.940	1.134	1.573	0.402	0.631	9.941
NGC 4111	2.213	0.92	2.208	84	0.652	2.415	2	1.443	1.194	1.382	1.823	0.302	0.639	9.973
NGC 4119	1.838	0.65	1.806	71	0.510	2.064	3	1.837	1.614	1.699	2.240	0.336	0.631	9.849
NGC 4143	2.252	0.99	2.250	64	0.749	2.488	1	1.349	1.255	1.332	1.740	0.453	0.324	9.911
NGC 4150	1.915	0.92	1.914	52	0.416	2.180	3	1.365	1.282	1.337	1.748	0.469	0.305	9.521
NGC 4168	2.232	0.58	2.241	87	0.902	2.483	0	1.566	1.537	1.681	2.175	0.398	0.109	10.398
NGC 4179	2.224	0.87	2.222	86	0.772	2.455	3	1.518	1.282	1.463	1.884	0.404	0.580	9.981
NGC 4191	2.095	1.00	2.109	90	0.658	2.366	1	1.231	1.156	1.311	1.728	0.440	0.295	10.046
NGC 4203	2.111	0.53	2.155	85	0.537	2.347	0	1.603	1.585	1.753	2.126	0.505	0.100	10.067
NGC 4215	2.124	0.94	2.142	90	0.609	2.401	2	1.402	1.171	1.368	1.747	0.424	0.600	10.126
NGC 4233	2.288	1.00	2.313	66	0.834	2.538	2	1.244	1.205	1.251	1.682	0.414	0.148	10.238
NGC 4249	1.901	0.99	1.880	85	0.540	2.122	0	1.174	1.167	1.295	1.740	0.432	0.037	9.671
NGC 4251	2.110	0.86	2.104	80	0.405	2.324	1	1.499	1.316	1.468	1.942	0.371	0.492	10.211
NGC 4255	2.203	0.99	2.206	70	0.811	2.483	3	1.142	1.030	1.176	1.555	0.457	0.294	9.905
NGC 4259	2.036	1.00	2.025	89	0.641	2.242	0	1.099	0.907	1.093	1.529	0.396	0.543	9.681
NGC 4261	2.424	0.46	2.466	89	0.929	2.671	1	1.687	1.651	1.808	2.229	0.456	0.169	10.793
NGC 4262	2.207	1.00	2.201	26	0.753	2.563	2	1.076	1.066	1.087	1.462	0.468	0.061	9.726
NGC 4264	2.029	1.00	2.027	38	0.603	2.280	0	1.161	1.126	1.172	1.693	0.350	0.151	9.952
NGC 4267	2.092	0.70	2.138	26	0.598	2.384	1	1.581	1.576	1.494	1.915	0.583	0.025	9.975
NGC 4268	2.188	0.99	2.174	88	0.853	2.408	1	1.250	1.104	1.299	1.709	0.407	0.426	9.889
NGC 4270	2.096	0.97	2.145	80	0.541	2.284	1	1.396	1.232	1.416	1.859	0.373	0.503	10.204
NGC 4278	2.328	0.79	2.358	88	0.829	2.561	1	1.542	1.524	1.672	2.084	0.458	0.087	10.247
NGC 4281	2.357	0.81	2.379	71	0.956	2.584	2	1.564	1.389	1.536	1.959	0.435	0.542	10.263
NGC 4283	2.000	1.00	1.994	26	0.570	2.242	1	1.078	1.076	1.192	1.656	0.381	0.022	9.457
NGC 4324	1.956	0.95	1.945	66	0.476	2.207	1	1.389	1.280	1.355	1.814	0.389	0.349	9.735
NGC 4339	1.980	0.69	2.044	26	0.685	2.275	0	1.489	1.475	1.553	1.974	0.444	0.068	9.748
NGC 4340	2.027	0.74	2.044	53	0.600	2.293	0	1.590	1.565	1.680	2.065	0.483	0.133	9.966
NGC 4342	2.384	0.99	2.374	90	1.017	2.610	3	0.975	0.757	0.954	1.345	0.411	0.558	9.504
NGC 4346	2.104	0.89	2.101	77	0.635	2.357	3	1.466	1.272	1.410	1.810	0.448	0.503	9.756
NGC 4350	2.242	0.86	2.223	89	0.771	2.472	3	1.502	1.229	1.435	1.860	0.393	0.662	9.949

Table 1 – continued

Galaxy	$\log \sigma_e$ (km s^{-1})	$R(\sigma)/R_e$	$\log \sigma_{\text{kpc}}$ (km s^{-1})	Inc ($^\circ$)	$\log(M/L)_{\text{JAM}}$ (M_\odot/L_\odot)	$\log V_{\text{circ}}^{\text{max}}$ (km s^{-1})	qual	$\log R_e^{\text{maj}}$ (arcsec)	$\log R_e$ (arcsec)	$\log r_{1/2}$ (arcsec)	$\log r_g$ (arcsec)	conc	ε_e	$\log L$ (L_\odot)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
NGC 4365	2.345	0.43	2.403	88	0.741	2.565	2	1.839	1.778	1.945	2.380	0.452	0.250	10.784
NGC 4371	2.158	0.60	2.171	76	0.705	2.382	1	1.559	1.544	1.685	2.165	0.419	0.106	10.106
NGC 4374	2.412	0.50	2.453	88	0.816	2.658	1	1.803	1.787	1.928	2.368	0.462	0.082	10.769
NGC 4377	2.092	1.00	2.093	41	0.514	2.344	0	1.190	1.162	1.279	1.641	0.503	0.120	9.732
NGC 4379	1.994	0.96	2.007	58	0.600	2.253	1	1.335	1.273	1.410	1.845	0.412	0.245	9.669
NGC 4382	2.253	0.31	2.269	90	0.629	2.512	0	1.978	1.918	2.067	2.530	0.416	0.240	10.819
NGC 4387	1.998	0.99	2.004	71	0.574	2.195	1	1.295	1.181	1.325	1.794	0.350	0.397	9.608
NGC 4406	2.280	0.21	2.342	89	0.754	2.519	1	2.154	2.095	2.267	2.713	0.440	0.239	10.846
NGC 4417	2.133	0.90	2.130	84	0.644	2.360	2	1.486	1.291	1.480	1.901	0.404	0.541	9.904
NGC 4425	1.918	0.79	1.915	90	0.606	2.089	0	1.619	1.349	1.552	2.032	0.331	0.683	9.612
NGC 4429	2.248	0.56	2.298	70	0.788	2.458	0	1.819	1.690	1.834	2.319	0.398	0.443	10.379
NGC 4434	1.999	1.00	2.038	43	0.417	2.223	1	1.175	1.163	1.297	1.710	0.441	0.067	9.793
NGC 4435	2.184	0.80	2.177	68	0.592	2.402	3	1.530	1.371	1.478	1.940	0.422	0.479	10.096
NGC 4442	2.231	0.83	2.259	72	0.672	2.469	3	1.472	1.377	1.485	1.932	0.404	0.344	10.145
NGC 4452	1.901	0.73	1.864	88	0.705	2.165	3	1.676	1.257	1.459	1.970	0.277	0.840	9.554
NGC 4458	1.947	0.90	1.967	84	0.527	2.136	1	1.359	1.332	1.474	1.900	0.433	0.119	9.505
NGC 4459	2.199	0.63	2.231	48	0.646	2.441	1	1.680	1.634	1.730	2.152	0.451	0.187	10.273
NGC 4461	2.106	0.86	2.124	71	0.642	2.368	3	1.476	1.356	1.461	1.861	0.438	0.385	9.910
NGC 4472	2.398	0.28	2.460	43	0.746	2.657	1	2.059	2.019	2.107	2.559	0.448	0.168	11.029
NGC 4473	2.271	0.81	2.277	81	0.715	2.517	2	1.604	1.473	1.652	2.048	0.481	0.436	10.213
NGC 4474	1.930	0.78	1.944	89	0.502	2.185	2	1.587	1.330	1.504	1.936	0.429	0.590	9.685
NGC 4476	1.880	0.99	1.886	88	0.464	2.115	0	1.318	1.222	1.384	1.855	0.407	0.367	9.537
NGC 4477	2.173	0.46	2.213	27	0.721	2.464	1	1.659	1.643	1.649	2.105	0.469	0.069	10.222
NGC 4478	2.140	0.98	2.156	41	0.714	2.424	3	1.241	1.198	1.259	1.735	0.327	0.189	9.854
NGC 4483	1.941	0.99	1.939	70	0.630	2.171	1	1.336	1.256	1.394	1.824	0.405	0.289	9.508
NGC 4486	2.422	0.39	2.487	84	0.858	2.647	2	1.917	1.897	2.043	2.522	0.403	0.083	10.869
NGC 4486A	2.091	1.00	2.089	42	0.656	2.345	1	0.979	0.935	1.000	1.474	0.365	0.159	9.535
NGC 4489	1.832	0.88	1.818	87	0.442	2.059	0	1.377	1.356	1.502	1.929	0.435	0.088	9.424
NGC 4494	2.176	0.59	2.196	86	0.599	2.394	1	1.704	1.670	1.813	2.283	0.403	0.148	10.394
NGC 4503	2.128	0.73	2.140	67	0.733	2.362	3	1.593	1.449	1.571	2.035	0.417	0.468	9.955
NGC 4521	2.269	0.97	2.237	90	0.851	2.466	3	1.368	1.168	1.356	1.811	0.346	0.553	10.269
NGC 4526	2.320	0.64	2.368	77	0.748	2.539	1	1.749	1.610	1.741	2.195	0.396	0.447	10.495
NGC 4528	2.007	1.00	2.001	57	0.583	2.264	2	1.149	1.064	1.073	1.541	0.376	0.254	9.540
NGC 4546	2.274	0.86	2.273	69	0.736	2.501	3	1.518	1.347	1.474	1.908	0.437	0.515	10.021
NGC 4550	2.062	0.93	2.036	81	0.706	2.289	3	1.434	1.195	1.374	1.836	0.296	0.653	9.690
NGC 4551	1.971	0.96	1.986	63	0.697	2.235	2	1.310	1.236	1.367	1.853	0.351	0.287	9.565
NGC 4552	2.351	0.49	2.388	90	0.811	2.606	2	1.629	1.613	1.752	2.153	0.493	0.073	10.391
NGC 4564	2.189	0.90	2.184	76	0.683	2.397	3	1.486	1.288	1.450	1.870	0.427	0.555	9.900
NGC 4570	2.223	0.88	2.217	88	0.689	2.472	3	1.503	1.253	1.460	1.859	0.410	0.621	10.073
NGC 4578	2.028	0.81	2.023	48	0.640	2.281	1	1.596	1.521	1.574	2.006	0.483	0.287	9.811
NGC 4596	2.099	0.50	2.165	37	0.677	2.392	2	1.767	1.730	1.660	2.157	0.450	0.160	10.237
NGC 4608	2.040	0.43	2.100	26	0.633	2.310	2	1.676	1.666	1.523	1.997	0.561	0.029	9.985
NGC 4612	1.935	0.83	1.936	58	0.403	2.194	0	1.506	1.459	1.577	2.020	0.432	0.191	9.862
NGC 4621	2.296	0.57	2.330	88	0.765	2.526	3	1.750	1.649	1.812	2.227	0.453	0.368	10.354
NGC 4623	1.884	0.82	1.856	89	0.657	2.076	1	1.582	1.315	1.520	1.986	0.350	0.684	9.513
NGC 4624	2.090	0.46	2.140	27	0.635	2.357	1	1.780	1.768	1.828	2.294	0.474	0.057	10.233
NGC 4636	2.259	0.27	2.297	89	0.905	2.502	0	2.034	1.972	2.133	2.601	0.432	0.231	10.491
NGC 4638	2.134	0.95	2.114	78	0.469	2.309	3	1.411	1.167	1.304	1.780	0.371	0.650	9.939
NGC 4643	2.171	0.56	2.205	25	0.682	2.490	2	1.565	1.555	1.671	2.051	0.459	0.050	10.210
NGC 4649	2.428	0.35	2.488	47	0.838	2.687	2	1.932	1.884	1.987	2.444	0.446	0.196	10.881
NGC 4660	2.263	1.00	2.259	74	0.688	2.475	2	1.242	1.111	1.252	1.666	0.442	0.409	9.811
NGC 4684	1.847	0.85	1.840	75	0.365	2.078	2	1.523	1.320	1.456	1.893	0.352	0.607	9.622
NGC 4690	1.991	0.97	2.036	51	0.590	2.264	1	1.352	1.290	1.388	1.846	0.421	0.247	10.030
NGC 4694	1.728	0.67	1.760	69	0.148	1.929	0	1.659	1.478	1.585	2.052	0.384	0.558	9.751
NGC 4697	2.229	0.39	2.256	70	0.704	2.439	3	1.959	1.851	1.990	2.429	0.433	0.400	10.364
NGC 4710	2.020	0.75	2.014	88	0.647	2.265	1	1.870	1.507	1.721	2.201	0.283	0.784	10.114
NGC 4733	1.717	0.78	1.739	88	0.339	1.909	0	1.567	1.554	1.682	2.205	0.331	0.076	9.538
NGC 4753	2.241	0.47	2.267	58	0.604	2.467	1	1.852	1.762	1.828	2.336	0.382	0.321	10.784
NGC 4754	2.204	0.85	2.231	60	0.679	2.446	2	1.551	1.486	1.542	2.008	0.462	0.260	10.132
NGC 4762	2.126	0.66	2.095	90	0.563	2.419	3	2.018	1.545	1.780	2.222	0.396	0.855	10.543
NGC 4803	2.023	1.00	2.011	89	0.685	2.277	0	1.044	0.943	1.094	1.591	0.328	0.376	9.753
NGC 5103	2.046	0.98	2.025	90	0.540	2.284	0	1.320	1.082	1.258	1.671	0.447	0.598	9.747

Table 1 – *continued*

Galaxy	$\log \sigma_e$ (km s^{-1})	$R(\sigma)/R_e$	$\log \sigma_{\text{kpc}}$ (km s^{-1})	Inc ($^\circ$)	$\log(M/L)_{\text{JAM}}$ (M_\odot/L_\odot)	$\log V_{\text{circ}}^{\text{max}}$ (km s^{-1})	qual	$\log R_e^{\text{maj}}$ (arcsec)	$\log R_e$ (arcsec)	$\log r_{1/2}$ (arcsec)	$\log r_g$ (arcsec)	conc	ε_e	$\log L$ (L_\odot)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
NGC 5173	1.986	1.00	1.993	44	0.413	2.270	0	1.082	1.050	1.157	1.592	0.433	0.140	10.002
NGC 5198	2.228	0.86	2.296	35	0.793	2.481	1	1.388	1.357	1.409	1.871	0.390	0.137	10.393
NGC 5273	1.824	0.70	1.851	35	0.517	2.159	1	1.620	1.580	1.454	1.931	0.389	0.165	9.732
NGC 5308	2.315	0.92	2.327	86	0.814	2.549	3	1.475	1.171	1.375	1.795	0.367	0.675	10.343
NGC 5322	2.351	0.58	2.391	90	0.688	2.589	1	1.730	1.646	1.813	2.233	0.464	0.318	10.844
NGC 5342	2.189	1.00	2.177	74	0.836	2.417	0	1.038	0.867	1.004	1.454	0.382	0.475	9.760
NGC 5353	2.449	0.89	2.427	80	0.838	2.642	2	1.474	1.278	1.438	1.931	0.342	0.557	10.665
NGC 5355	1.943	1.00	1.944	69	0.553	2.186	0	1.083	1.043	1.180	1.639	0.377	0.170	9.765
NGC 5358	1.938	1.00	1.897	81	0.678	2.189	0	1.105	0.935	1.112	1.581	0.351	0.456	9.598
NGC 5379	1.956	0.92	1.840	89	0.875	2.153	1	1.438	1.240	1.422	1.960	0.294	0.598	9.557
NGC 5422	2.197	0.88	2.209	90	0.785	2.450	1	1.486	1.251	1.453	1.852	0.417	0.584	10.164
NGC 5473	2.257	0.87	2.297	39	0.684	2.532	0	1.385	1.351	1.378	1.811	0.494	0.142	10.404
NGC 5475	2.061	0.96	2.010	79	0.678	2.291	2	1.410	1.153	1.319	1.731	0.380	0.644	9.887
NGC 5481	2.085	0.87	2.134	53	0.776	2.379	0	1.401	1.348	1.450	1.854	0.486	0.203	9.837
NGC 5485	2.223	0.69	2.241	87	0.847	2.443	0	1.511	1.461	1.617	2.078	0.409	0.206	10.208
NGC 5493	2.296	0.95	2.248	76	0.471	2.460	3	1.389	1.161	1.291	1.695	0.458	0.626	10.494
NGC 5500	1.924	0.99	1.937	88	0.713	2.171	0	1.266	1.212	1.360	1.808	0.429	0.221	9.618
NGC 5507	2.216	0.99	2.235	63	0.825	2.472	3	1.117	1.078	1.086	1.501	0.441	0.157	9.904
NGC 5557	2.306	0.71	2.386	88	0.662	2.531	1	1.480	1.449	1.598	2.010	0.459	0.139	10.671
NGC 5574	1.907	0.99	1.913	89	0.399	2.100	0	1.307	1.120	1.301	1.784	0.355	0.571	9.705
NGC 5576	2.191	0.70	2.242	62	0.453	2.442	2	1.526	1.448	1.587	1.976	0.513	0.306	10.426
NGC 5582	2.170	0.69	2.172	55	0.722	2.418	1	1.551	1.461	1.563	1.944	0.508	0.336	10.140
NGC 5611	2.138	0.99	2.125	74	0.697	2.360	3	1.114	0.936	1.082	1.488	0.437	0.528	9.652
NGC 5631	2.176	0.79	2.196	87	0.626	2.439	0	1.434	1.408	1.552	1.931	0.481	0.119	10.261
NGC 5638	2.160	0.70	2.188	66	0.667	2.387	0	1.472	1.455	1.593	2.054	0.415	0.077	10.260
NGC 5687	2.216	0.74	2.244	87	0.907	2.454	1	1.537	1.420	1.602	1.995	0.489	0.397	10.064
NGC 5770	1.905	0.99	1.933	26	0.385	2.213	0	1.205	1.205	1.354	1.687	0.473	0.003	9.603
NGC 5813	2.324	0.51	2.355	89	0.875	2.589	0	1.792	1.727	1.884	2.322	0.440	0.247	10.717
NGC 5831	2.158	0.85	2.204	86	0.667	2.380	0	1.468	1.441	1.587	2.021	0.445	0.129	10.203
NGC 5838	2.350	0.81	2.391	70	0.900	2.592	3	1.483	1.374	1.424	1.886	0.449	0.362	10.257
NGC 5839	2.098	0.98	2.131	88	0.720	2.360	0	1.270	1.256	1.400	1.763	0.529	0.079	9.700
NGC 5845	2.357	1.00	2.327	63	0.695	2.530	3	0.764	0.706	0.825	1.278	0.353	0.254	9.792
NGC 5846	2.349	0.52	2.364	89	0.908	2.558	1	1.787	1.773	1.919	2.398	0.407	0.059	10.665
NGC 5854	2.020	0.96	2.009	74	0.421	2.223	3	1.375	1.200	1.303	1.751	0.368	0.502	10.025
NGC 5864	2.035	0.85	2.044	74	0.570	2.260	3	1.525	1.283	1.397	1.849	0.323	0.647	10.136
NGC 5866	2.196	0.52	2.212	76	0.665	2.428	0	1.775	1.582	1.743	2.224	0.335	0.579	10.336
NGC 5869	2.224	0.89	2.242	80	0.849	2.462	1	1.405	1.343	1.505	1.899	0.471	0.247	10.033
NGC 6010	2.202	0.91	2.179	90	0.772	2.428	1	1.454	1.147	1.377	1.759	0.415	0.687	10.045
NGC 6014	1.946	0.85	1.951	32	0.649	2.273	0	1.398	1.372	1.232	1.746	0.369	0.114	9.929
NGC 6017	2.051	1.00	2.058	74	0.447	2.257	1	1.072	0.922	1.067	1.483	0.442	0.481	9.734
NGC 6149	2.021	1.00	2.016	66	0.663	2.271	0	1.119	1.039	1.191	1.611	0.427	0.305	9.772
NGC 6278	2.295	1.00	2.307	66	0.741	2.526	0	1.274	1.149	1.296	1.646	0.493	0.411	10.283
NGC 6547	2.257	1.00	2.231	84	0.824	2.520	1	1.264	1.023	1.231	1.617	0.459	0.598	10.091
NGC 6548	2.153	0.65	2.210	19	0.867	2.430	1	1.562	1.554	1.551	2.028	0.558	0.030	10.001
NGC 6703	2.178	0.63	2.236	18	0.776	2.468	1	1.489	1.485	1.604	1.976	0.474	0.020	10.200
NGC 6798	2.114	1.00	2.121	84	0.660	2.349	2	1.226	1.093	1.267	1.729	0.404	0.415	10.028
NGC 7280	2.024	0.92	2.039	58	0.545	2.322	1	1.423	1.331	1.470	1.809	0.514	0.350	9.853
NGC 7332	2.097	0.97	2.106	84	0.336	2.339	1	1.426	1.194	1.385	1.778	0.413	0.590	10.201
NGC 7454	2.058	0.85	2.065	88	0.733	2.272	0	1.462	1.379	1.530	2.017	0.388	0.330	9.894
NGC 7457	1.873	0.67	1.870	74	0.482	2.065	1	1.712	1.574	1.736	2.278	0.348	0.462	9.736
NGC 7465	1.981	1.00	1.991	88	0.373	2.213	0	1.054	0.964	1.119	1.588	0.356	0.311	9.827
NGC 7693	1.763	1.00	1.766	42	0.588	2.045	1	1.150	1.092	1.039	1.541	0.384	0.214	9.409
NGC 7710	1.957	1.00	1.954	77	0.536	2.173	1	0.960	0.784	0.903	1.399	0.302	0.487	9.523
PGC 016060	2.043	1.00	1.963	77	0.651	2.240	2	1.203	0.940	1.016	1.486	0.277	0.661	9.795
PGC 028887	2.109	1.00	2.122	90	0.876	2.373	0	1.085	1.012	1.183	1.554	0.525	0.297	9.658
PGC 029321	1.822	1.00	1.802	32	0.492	2.078	0	0.860	0.837	0.908	1.317	0.336	0.113	9.350
PGC 035754	2.015	1.00	2.031	58	0.578	2.264	1	1.009	0.942	1.064	1.469	0.491	0.291	9.658
PGC 042549	2.009	1.00	1.992	54	0.500	2.278	1	1.003	0.921	0.954	1.398	0.429	0.318	9.806
PGC 044433	2.087	1.00	2.075	89	0.790	2.355	1	0.936	0.762	0.957	1.374	0.373	0.466	9.643
PGC 050395	1.909	1.00	1.860	86	0.574	2.146	0	1.058	0.996	1.147	1.594	0.430	0.248	9.571
PGC 051753	1.949	1.00	1.912	89	0.686	2.156	1	1.103	0.926	1.095	1.596	0.291	0.548	9.535
PGC 054452	1.803	0.98	1.800	41	0.562	2.061	1	1.173	1.121	1.091	1.601	0.379	0.212	9.429

Table 1 – continued

Galaxy	$\log \sigma_e$ (km s ⁻¹)	$R(\sigma)/R_e$	$\log \sigma_{\text{kpc}}$ (km s ⁻¹)	Inc (°)	$\log(M/L)_{\text{JAM}}$ (M _⊙ /L _{⊙,r})	$\log V_{\text{circ}}^{\text{max}}$ (km s ⁻¹)	qual	$\log R_e^{\text{maj}}$ (arcsec)	$\log R_e$ (arcsec)	$\log r_{1/2}$ (arcsec)	$\log r_g$ (arcsec)	conc	ε_e	$\log L$ (L _{⊙,r})
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
PGC 056772	1.932	1.00	1.915	64	0.621	2.163	1	1.129	0.982	1.062	1.559	0.324	0.486	9.623
PGC 058114	2.004	1.00	2.021	–	–	–	–	–	–	–	–	–	–	–
PGC 061468	1.884	1.00	1.823	86	0.841	2.141	0	1.090	1.029	1.188	1.781	0.280	0.248	9.397
PGC 071531	1.979	1.00	1.968	–	–	–	–	–	–	–	–	–	–	–
PGC 170172	1.836	1.00	1.901	88	0.245	2.072	0	0.893	0.835	0.978	1.379	0.461	0.250	9.559
UGC 03960	1.919	0.88	1.939	87	0.738	2.171	0	1.396	1.340	1.498	1.910	0.475	0.203	9.652
UGC 04551	2.219	1.00	2.223	76	0.687	2.445	2	0.936	0.902	1.024	1.477	0.326	0.146	9.878
UGC 05408	1.781	1.00	1.780	26	0.197	2.086	0	0.768	0.765	0.729	1.227	0.429	0.012	9.655
UGC 06062	2.125	1.00	2.148	60	0.764	2.362	1	1.069	1.018	1.133	1.595	0.409	0.216	9.864
UGC 06176	1.984	0.99	1.991	63	0.685	2.320	0	1.014	0.988	1.005	1.504	0.398	0.102	9.751
UGC 08876	2.105	1.00	2.114	90	0.759	2.405	1	0.984	0.835	1.040	1.413	0.440	0.421	9.686
UGC 09519	2.001	1.00	1.990	68	0.559	2.239	1	1.008	0.870	1.007	1.425	0.427	0.451	9.504

Note. – column (1): the Name is the principal designation from LEDA (Paturel et al. 2003), which is used as standard designation for our project. Column (2): effective stellar velocity dispersion (1σ error of 5 per cent or 0.021 dex). This is measured by co-adding all SAURON spectra contained within the ‘effective’ ellipse with area $A_e = \pi R_e^2$ (column 10) and ellipticity ε_e (column 14), with major axis aligned along the kinematic position angle PA_{kin} from table D1 of Paper II. The velocity dispersion is measured on that single spectrum using PPXF. For this reason σ_e includes both the effects of stellar rotation and random motions. Column (3): $R(\sigma)/R_e \equiv \sqrt{A_{\text{obs}}/A_e}$, where $A_{\text{obs}} \leq A_e$ is the area of the effective ellipse covered by the SAURON observations. When this ratio is < 1 then σ_e was corrected with equation 1 of Cappellari et al. (2006). Column (4): same as in column 2 (same error as σ_e), for the σ measured within a fixed circular aperture of radius $R = 1$ kpc. Column (5): Inclination of the best-fitting mass-follow-light JAM models. Errors are dominated by systematics and difficult to assess on an individual basis. For good models (column 8), the inclination errors are generally smaller than 5° (also see Paper XII). Column (6): Mass-to-light ratio (1σ error of 6 per cent or 0.027 dex) of the best-fitting self-consistent JAM model (A) for the assumed distance and extinction of table 3 of Paper I. This is the scaling factor by which the surface brightness in solar luminosities has to be multiplied, to best reproduce the observed stellar kinematics. $(M/L)_{\text{JAM}} \approx (M/L)(r = R_e)$ approximates the total M/L measured within a spherical region of radius R_e (Section 4.1.2). By definition the quantity $M_{\text{JAM}} \equiv (M/L)_{\text{JAM}} \times L$ (column 15). Column (7): maximum value of the circular velocity predicted by the best-fitting mass-follow-light JAM model. Although the model does not explicitly include dark matter, V_{circ} is due to the total mass density, not by the stars alone. Column (8): visual description of the quality of the self-consistent JAM model fit (see Fig. 1). $\text{qual} = 0$ indicates inferior data quality (low S/N) or a problematic model (e.g. due to the presence of a strong bar or dust, or genuine kinematic twists). The $(M/L)_{\text{JAM}}$ may be less accurate in this case (see Paper XII). $\text{qual} = 1$ indicates an acceptable fit to the V_{rms} . $\text{qual} = 2$ indicates a good fit to the V_{rms} . Every feature of the data is accurately predicted by the JAM model. $\text{qual} = 3$ indicates that not only the data and the fit to the V_{rms} are good, but also both V and σ (not shown) can be accurately predicted by the JAM model, without more free parameters. Column (9): maximum dimension (major axis) of the isophote containing half of the analytic total light of the MGE models of Paper XXI (1σ error of 10 per cent or 0.041 dex). Column (10): $R_e \equiv \sqrt{A_e/\pi}$ where A_e is the area of the effective isophote containing half of the analytic total light of the MGE models (same error as R_e^{maj}). Column (11): radius $r_{1/2} = [3V_e/(4\pi)]^{1/3}$ of a sphere that has the same volume V_e of the isosurface enclosing half of the total galaxy light. Column (12): gravitational radius calculated from the MGE model using equation (18). Column (13): Galaxy concentration $\text{conc} \equiv L(R_e/3)/L(R_e)$ (Trujillo et al. 2001), where $L(R)$ is the light of the circularized MGE model contained within the radius R . Column (14): ellipticity of the galaxy light distribution. This is calculated from the moment of inertia of the MGE model within the effective isophote using equation (12). Column (15): analytic total luminosity (1σ error of 10 per cent or 0.041 dex) of the MGE model in the SDSS r band at the assumed distance and extinction given in table 3 of Paper I, for an assumed absolute solar magnitude $M_{\odot,r} = 4.64$ mag (Blanton & Roweis 2007). Table 1 is also available from our project website <http://purl.org/atlas3d>.

halo density ρ_s at r_s , which we parametrized using the dark matter fraction $f_{\text{DM}}(r = R_e)$ to reduce the strong correlation between ρ_s and γ during the parameter estimation. The break radius r_s of the halo was not included as a free parameter given that it is (in models E) generally three to five times larger than R_e and it is completely unconstrained by our data. We fixed $r_s = 20$ kpc, which is the median value for all models E, but we verified that nearly identical results are obtained if we describe the halo with a simple power-law density profile $\rho(r) \propto r^{-\gamma}$. Examples of model fits are shown in Fig. 3.

(E) *JAM with fixed NFW dark halo*. The halo has an NFW profile without any free parameter. During the fitting process the halo mass M_{200} is determined from the enclosed stellar mass M_{stars} , which is given by the total luminosity of the MGE model multiplied by its current $(M/L)_{\text{stars}}$. This is done using the $M_{200}-M_{\text{stars}}$ relation derived by Moster et al. (2010) (see also Moster, Naab & White 2013), which matches the observed galaxy luminosity functions to the simulated haloes mass function. However, negligible differences would have been obtained using e.g. the similar relations derived by Behroozi, Conroy & Wechsler (2010) or Guo et al. (2010). For a given halo mass, the concentration is specified by the $M_{200}-c_{200}$ relation as in (B). The only free model parameters are the three of

the stellar component ($i, \beta_z, (M/L)_{\text{stars}}$) as in (A). This fixed-halo assumption, in combination however with equally fixed spherical and isotropic Hernquist (1990) galaxy models, was also used by Auger et al. (2010a) and Deason et al. (2012).

(F) *JAM with fixed contracted dark halo*. The halo has a contracted profile without any free parameter. For a given stellar mass, the halo has initially the same NFW form as in (E), but the profile is contracted as in (C) using the prescription of Gnedin et al. (2011). The only free model parameters are the three of the stellar component ($i, \beta_z, (M/L)_{\text{stars}}$) as in (A). This fixed-halo assumption, in combination however with equally fixed spherical and isotropic Hernquist (1990) galaxy models, was also used by Auger et al. (2010a).

3.1.3 Bayesian inference of the JAM model parameters

The determination of the JAM model parameters for the 260 ATLAS^{3D} galaxies in Cappellari et al. (2012) was done using Bayesian inference (Gelman et al. 2004). The same approach was adopted using JAM models in Barnabè et al. (2012) in combination with gravitational lensing. From Bayes theorem, the posterior probability distribution of a model, with a given set of parameters,

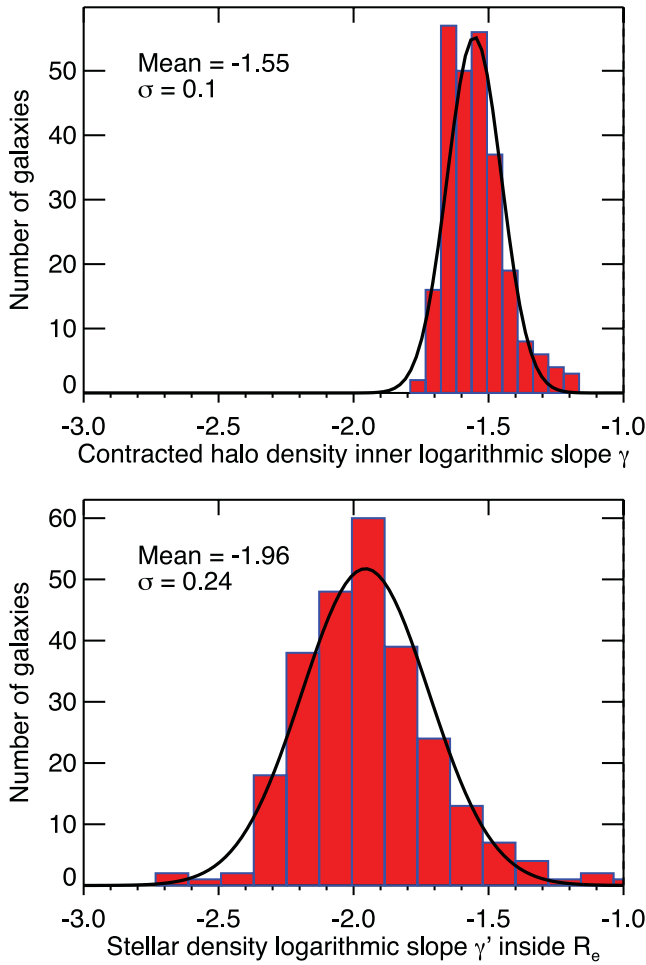


Figure 2. Inner slope of contracted dark haloes and luminous matter. Top panel: histogram of the halo slope of contracted haloes for all 260 ATLAS^{3D} galaxies in model (C). The slopes were determined by fitting a power-law relation $\rho_{\text{DM}}(r) \propto r^{\gamma'}$ inside the radius $r < r_s/4$, where we verified that the contracted halo profiles are accurately described by a power law. Bottom panel: histogram of the slope of the deprojected stellar mass density distribution from the MGE models. The slope was fitted inside a spherical radius $r = R_e$. Although the stellar density $\rho_*(r) \propto r^{\gamma'}$ inside that radius is not always accurately described by a power law, on average the stellar slope peaks with high accuracy at the ‘isothermal’ value $\gamma' \approx 2.0$, with an intrinsic scatter of just $\sigma = 0.24$ for our entire sample.

given our data is

$$P(\text{model} | \text{data}) \propto P(\text{data} | \text{model}) \times P(\text{model}). \quad (3)$$

Here, we make the rather common assumption of Gaussian errors, in which case the probability of the data, for a given model is given by

$$P(\text{data} | \text{model}) \propto \exp\left(-\frac{\chi^2}{2}\right), \quad (4)$$

with

$$\chi^2 = \sum_j \left(\frac{(v_{\text{los}}^2)_j^{1/2} - V_{\text{rms},j}}{\Delta V_{\text{rms},j}} \right)^2. \quad (5)$$

We further assume a constant *non-informative* prior $P(\text{model})$ for all variables within the given bounds.

The calculation of the posterior distribution is performed using the *adaptive* Metropolis et al. (1953) (AM) algorithm of Haario,

Saksman & Tamminen (2001). The AM method adapts the multivariate Gaussian proposal distribution during the Markov chain Monte Carlo sampling, in such a way that the Gaussian proposal distribution has the same non-diagonal covariance matrix as the posterior distribution accumulated so far by the algorithm. This natural idea is similar to what is routinely done e.g. in the determination of cosmological parameters, where the covariance matrix of the posterior is calculated after a burn-in phase (e.g. Dunkley et al. 2005). However, the adaptive approach converges much more rapidly as the proposal distribution starts approaching the posterior already after a few points have been sampled. We found the adaptive approach absolutely critical for the speed up of our calculation by orders of magnitudes, given the strong degeneracies between the model parameters producing inclined and narrow posterior distributions. Some examples of the posterior distributions obtained with our approach are shown in Fig. 3. Although the adaptive nature of the AM algorithm makes the resulting chain non-Markovian, the authors have proven that it has the correct ergodic properties (Haario et al. 2001) and for this reason it can be used to estimate the posterior distribution as in standard Markov chain Monte Carlo methods (Gilks, Richardson & Spiegelhalter 1996).

Moreover, to basically eliminate the burn-in phase of the AM method, we use the efficient and extremely robust DIRECT deterministic global optimization algorithm of Jones, Perttunen & Stuckman (1993) to find the starting location without the risk for the Metropolis stage to be stuck in a possible secondary minimum in multidimensional parameter space.

An important addition to the fitting process is an iterative σ -clipping of the kinematics, to remove spurious features in the data, for example stars or problematic bins at the edge of the SAURON field of view. This is important for a sample of the size of ATLAS^{3D}, where the quality of every Voronoi bin cannot be assessed manually for all galaxies. After an initial fit the few bins deviating more than 3σ of the local rms noise are excluded from the fit and a new fit is iteratively performed, until convergence.

3.2 Robust fitting of lines or planes to the data

3.2.1 Goodness-of-fit criteria

The apparently simple task of fitting linear relations or planes to a set of data with errors does not have a well-defined and obvious solution and for this reason has continued to generate significant interest. A number of papers have discussed the solution of the corresponding least-squares problem (Isobe, Feigelson & Nelson 1986; Feigelson & Babu 1992; Akritas & Bershady 1996; Tremaine et al. 2002; Press et al. 2007), while more recent works have addressed the problem using Bayesian methods (Kelly 2007; Hogg, Bovy & Lang 2010). A popular method is the least-squares approach by Tremaine et al. (2002), which is an extension of the FITEXY procedure described in Press et al. (2007, section 15.3). The method defines the best fit of the linear relation $y = a + b(x - x_0)$ to a set of N pairs of quantities (x_j, y_j) , with symmetric errors Δx_j and Δy_j , as the one that minimizes the quantity

$$\chi^2 = \sum_{j=1}^N \frac{[a + b(x_j - x_0) - y_j]^2}{(b\Delta x_j)^2 + (\Delta y_j)^2 + \varepsilon_y^2}. \quad (6)$$

Here, x_0 is an adopted reference value, close to the middle of the x_j values, adopted to reduce uncertainty in a and the covariance between the fitted values of a and b . While ε_y is the intrinsic scatter in the y -coordinate, which is iteratively adjusted so that the χ^2 per

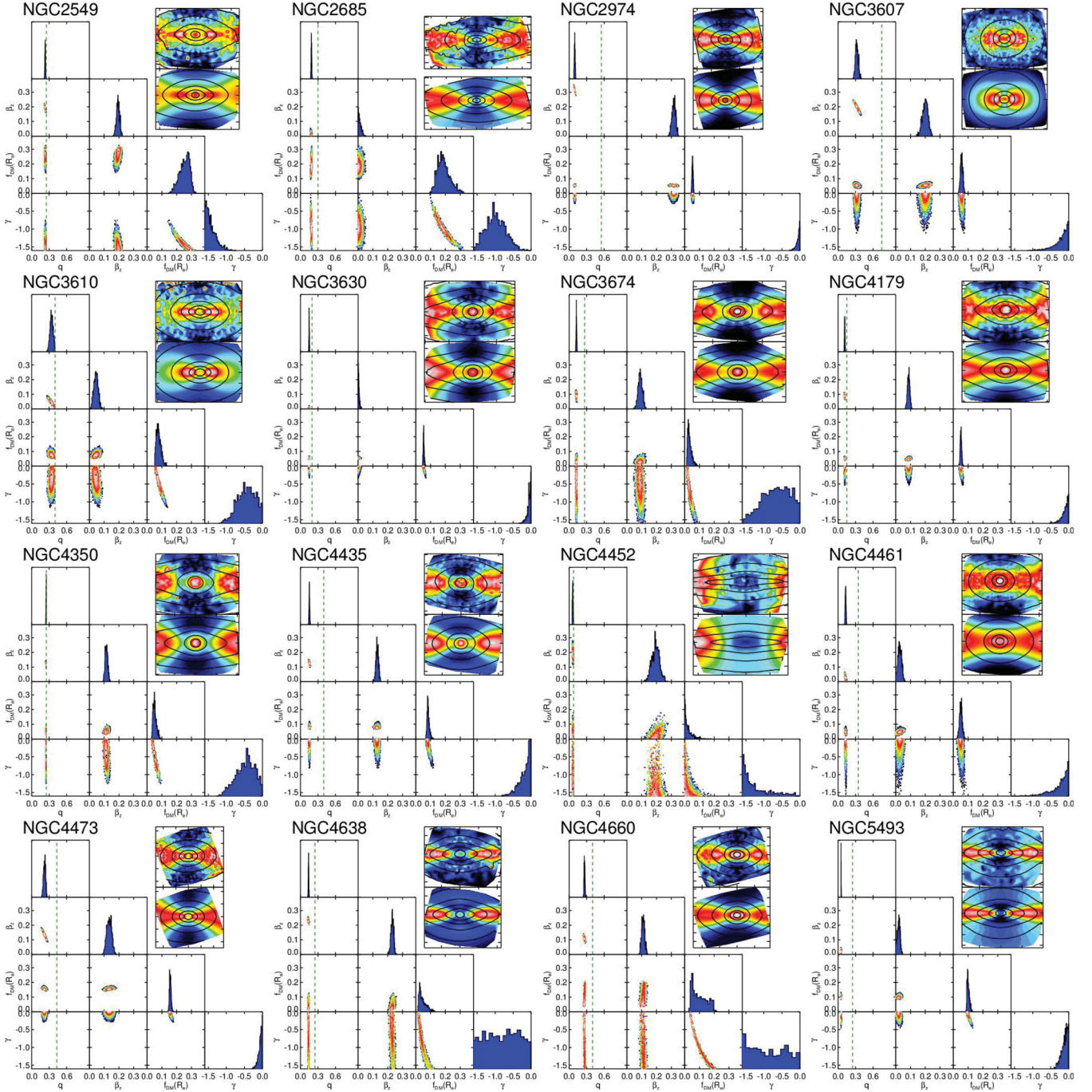


Figure 3. Examples of JAM dynamical modelling with general dark halo using an AM approach. Each panel shows the corner-plots of the posterior probability distribution for the non-linear model parameters (q , β_z , f_{DM} , γ), of galaxy models (D), marginalized over two dimensions (colour contours) and one dimension (blue histograms). The symbols are coloured according to their likelihood: white corresponds to the maximum value and dark blue to a 3σ confidence level. The vertical dashed green line indicates the maximum allowed q , which corresponds to an edge-on view. For each combination of the non-linear parameters, the linear parameter $(M/L)_{stars}$ is fitted to the data. We assumed ignorant (constant) priors on all model parameters. The name of the galaxies is written at the top of each panel. The symmetrized V_{rms} SAURON data, and the best-fitting model are shown on the right (as in Fig. 1). This plot illustrates a variety of situations and shapes of the kinematic field: (i) some models (NGC 2685, NGC 3610, NGC 3674, NGC 4350) have best-fitting halo parameters within the explored parameters boundaries; (ii) others (NGC 2974, NGC 3607, NGC 3630, NGC 4179, NGC 4435, NGC 4461, NGC 4473, NGC 5493) prefer a flat $\gamma \approx 0$ inner halo slope; (iii) others (NGC 4638, NGC 4660) have nearly unconstrained halo slope; (iv) others (NGC 2549, NGC 4452) prefer steep halo slopes at the boundary $\gamma = -1.6$ of our allowed parameter range. In all cases, the halo slope is weakly constrained by the SAURON data, but the dark matter fraction is tightly constrained by the data to be small ($f_{DM} \lesssim 25$ per cent in these examples). To include significant dark matter within $1R_e$ in some of the models, while still reproducing the kinematic observations, the inner dark halo slope would have to be as steep as the characteristic stellar density slope $\gamma' \approx -2.0$ (Fig. 2).

degree of freedom $\nu = N - 2$ has the value of unity expected for a good fit. As recognized by Weiner et al. (2006), minimizing the above χ^2 corresponds to maximizing the likelihood of the data for an assumed intrinsic probability distribution of the observables described by the linear relation $y = a + b(x - x_0) + \varepsilon_y$, where ε_y is the Gaussian scatter projected along the y -coordinate, and one assumes a uniform prior in the x -coordinate. Equation (6) is only rigorously valid when the errors in x and y are Gaussian and uncorrelated (have zero covariances). A term $-2b \text{Cov}(x_j, y_j)$ should be included in the denominator if the covariances are known and non-zero (e.g. Falcón-Barroso et al. 2011). The 1σ confidence interval in ε_y can be obtained by finding the values for which $\chi^2 = \nu \pm \sqrt{2\nu}$, as done by Novak, Faber & Dekel (2006). The apparent asymmetry of equation (6) with respect to the x and y variables does not imply we assume only the y variable has intrinsic scatter. In fact, the assumed intrinsic distribution has a Gaussian cross-section along any direction non-parallel to the ridge line $y = a + b(x - x_0)$. The value ε_y merely specifies the dispersion along the arbitrary y -direction. The formula would give completely equivalent results by interchanging the x and y variables if the distribution of x values was uniform and infinitely extended as assumed. Any difference in the fitting results when interchanging the x and y coordinates are due to the breaking of the uniformity assumptions.

Equation (6) can be generalized to plane fitting by defining the best-fitting plane $z = a + b(x - x_0) + c(y - y_0)$ to a set of N triplets of quantities (x_j, y_j, z_j) , with symmetric errors Δx_j , Δy_j and Δz_j , as the one that minimizes the quantity

$$\chi^2 = \sum_{j=1}^N \frac{[a + b(x_j - x_0) + c(y_j - y_0) - z_j]^2}{(b\Delta x_j)^2 + (c\Delta y_j)^2 + (\Delta z_j)^2 + \varepsilon_z^2}, \quad (7)$$

Here, x_0 and y_0 are adopted reference values, close to the middle of the x_j and y_j values, respectively, adopted to reduce uncertainty in a and the covariance between the fitted values of a , b and c . While ε_z is the intrinsic scatter in the z -coordinate, which is iteratively adjusted so that the χ^2 per degrees of freedom $\nu = N - 3$ has the value of unity expected for a good fit. As in the two-dimensional case, the minimization of equation (7) is equivalent to the maximization of the likelihood of the data, for an underlying probability distribution of the observables described by the relation $z = a + b(x - x_0) + c(y - y_0) + \varepsilon_z$, where ε_z is the dispersion of the Gaussian intrinsic scatter in the plane, projected along the z -coordinate, for a uniform prior in the x and y coordinates and assuming uncorrelated and Gaussian errors in the x , y and z observables (zero covariances). Equation (7) reduces to the so-called orthogonal plane fit when the measurements errors are ignored and one simply assumes $\Delta x_j = \Delta y_j = \Delta z_j$. This latter form is the one generally used when fitting the FP (e.g. Jorgensen, Franx & Kjaergaard 1996; Pahre, Djorgovski & de Carvalho 1998; Bernardi et al. 2003). Contrary to the popular approach, equation (7) allows for intrinsic scatter in the relation, which is important for deriving unbiased parameters (Tremaine et al. 2002).

Recently, Kelly (2007) proposed a Bayesian method to treat the linear regression of astronomical data in a statistically rigorous manner, allowing for intrinsic scatter, covariance between measurements and providing rigorous errors on the parameters in the form of random draws from the posteriori distribution (see also Hogg et al. 2010). He pointed out that the Tremaine et al. (2002) approach to linear fitting can lead to biased results in some circumstances. For this reason, in all our fits we used both the results and errors derived from equations (6) and (7), and the corresponding results obtained with the Bayesian method and software by Kelly (2007),

which was kindly made available as part of the IDL NASA Astronomy Library (Landsman 1993). In all cases, differences between the two methods were found to be insignificant, in both the fitted values and the errors, confirming the near-conceptual equivalence of the two technically very different approaches.

3.2.2 Least trimmed squares robust fits

A general issue when fitting linear relations to data using least-squares methods is the presence of outliers, which can dominate the χ^2 and bias the parameter recovery. This is the reason why a number of previous studies have determined the parameters of the FP using the more robust method of minimizing absolute instead of squared deviations (e.g. Jorgensen et al. 1996; Pahre et al. 1998), at the expense of decreasing the statistical efficiency, namely larger errors on the fitted parameters. An alternative simple solution, which maintains the efficiency of the least-squares method for Gaussian distributions, consists of removing outliers by iteratively clipping points deviating more than 3σ from the currently best-fitting relation. A problem with the σ -clipping approach is that it is not guaranteed to converge to the desired solution in the presence of significant outliers. Alternative robust methods have been proposed (see Press et al. 2007, section 15.7). However, they complicate the error estimation and like the standard σ -clipping do not always converge.

After some experimentation with different robust approaches the only fully satisfactory solution we found is the least trimmed squares (LTS) regression approach of Rousseeuw & Leroy (1987). The reason for its success is that the method, as opposed to other robust approaches, finds a *global* solution. The approach consists of finding the global minimum to

$$\chi_h^2 = \sum_{j=1}^h (r^2)_{j:N}, \quad (8)$$

where $(r^2)_{1:N} \leq (r^2)_{2:N} \leq \dots \leq (r^2)_{N:N}$ are the ordered square residuals from the linear regression of a subset of $N/2 < h < N$ data points. In other words, the LTS method consists of finding the subset of h data points providing the smallest χ_h^2 , among *all* possible h -subsets. It is easy to realize that this approach is robust to the contamination of up to half of the data points, when $h \approx N/2$. This is a computationally very expensive combinatorial problem for which however a fast and nearly optimal solution (FAST-LTS) has recently been proposed by Rousseeuw & Van Driessen (2006).

In our implementations,² which we called `LTS_LINEFIT` and `LTS_PLANEFIT` for the line and plane case, respectively, we combine the robust approach to outliers with a fitting method which allows and fits for intrinsic scatter. We proceed as follows:

- (i) we adopt as initial guess $\varepsilon = 0$ for the intrinsic scatter in the y (for `LTS_LINEFIT`) or z coordinate (for `LTS_PLANEFIT`);
- (ii) we start by default with $h = (N + p + 1)/2$, where p is the data dimension, and use the FAST-LTS algorithm to produce a least-squares fit³ to the set of points characterized by the smallest χ_h^2 (defined by equation 6 or 7);

² Available from <http://purl.org/cappellari/idl>

³ In all the non-linear fits, the minimization was performed with the IDL program `MPFIT` by Markwardt (2009), which is in an improved implementation of the MINPACK Levenberg–Marquardt non-linear least-squares algorithm by Moré, Garbow & Hillstrome (1980).

- (iii) we compute the standard deviation σ of the residuals for these h values and extend our selection to include all data point deviating no more than 2.6σ from the fitted relation (99 per cent of the values for a Gaussian distribution);
- (iv) we perform a new linear fit to the newly selected points;
- (v) we iterate steps (iii)–(iv) until the set of selected points does not change any more;
- (vi) we calculate the χ^2 for the fitted points;
- (vii) the whole process (i)–(vi) is iterated varying ε using Brent’s method (Press et al. 2007, section 9.3) until $\chi^2 = \nu$.
- (viii) the errors on the coefficients are computed from the covariance matrix;
- (ix) the error on ε is computed by increasing ε until $\chi^2 = \nu - \sqrt{2\nu}$ (we do not decrease it to avoid problems when $\varepsilon \approx 0$).

This method was used to produce all fits in this paper and automatically exclude outliers. Note that although the approach may appear similar to the standard σ -clipping one, and produces similar results in simple situations, the key difference is that in `LTS_LINEFIT` and `LTS_PLANEFIT` the clipping is done from the inside-out instead of the opposite. This was found to be the essential feature for the resulting extreme robustness, which was essential in particular to objectively select Virgo members in Fig. 16. Once the outliers are removed, the same set of points was used as input to Kelly (2007) Bayesian algorithm.

3.3 Measuring scaling relations parameters

3.3.1 Determination of L , R_e and $r_{1/2}$ from the MGE

Galaxy photometric parameters are generally determined using three main approaches: (i) fitting growth curves, where one constructs profiles of the enclosed light within circular annuli and extrapolates the outermost part of the galaxy profile to infinite radius, typically using the analytic growth curve of the $R^{1/4}$ (de Vaucouleurs 1948) profile (e.g. the Seven Samurai; Burstein et al. 1987; Faber et al. 1989; the RC3; de Vaucouleurs et al. 1991; Jorgensen, Franx & Kjaergaard 1995a); (ii) fitting an $R^{1/n}$ (Sérsic 1968) profile (e.g. Graham & Colless 1997), possibly including an exponential disc (e.g. Saglia et al. 1997), to the circularized profiles and finding the half-light from the models; (iii) fitting flattened two-dimensional models directly to the galaxy images, where the profile of the models is again parametrized by an $R^{1/4}$ (e.g. Bernardi et al. 2003), or by an $R^{1/4}$ bulge plus exponential disc (e.g. Gebhardt et al. 2003; Bernardi et al. 2010; Saglia et al. 2010).

Here, we have MGE photometric models for all the galaxies in the sample based on the SDSS+INT photometry (Paper XXI). Due to the large number of Gaussians used to fit the galaxy images, the MGE models provide a compact and essentially non-parametric description of the galaxies surface brightness, which reproduces the observations much more accurately than the simpler bulge and disc models, but more robustly than using the images directly. Our MGE fitting approach (Cappellari 2002) is in fact an efficient analogue to the popular `GALFIT` (Peng et al. 2002) software, when it is used to match every detail of a galaxy image using multiple components. Here, we use the MGE models to measure the photometric parameters (L and R_e) in our scaling relations as done in Cappellari et al. (2009). A key difference between this MGE approach and all the ones previously mentioned is that it does not extrapolate the galaxy light to infinite radii. Outside three times the dispersion $3 \max(\sigma_j)$ of the largest MGE Gaussian, the flux of the model essentially drops to zero. No attempt is made to infer the amount of stellar light that

we may have observed if we had much deeper photometry. For this reason, this R_e must be necessarily smaller than the ones obtained via extrapolation to infinite radii.

The extrapolation method depends on the assumed form of the unobservable galaxy profile out to infinite radii. One may argue that an extrapolation of the galaxy profile using a Sérsic (1968) function should provide a better estimate of the total luminosity (and R_e) than the observed luminosity. This is in general likely correct; however, the accuracy of the extrapolation depends on galaxy properties in a unknown systematic manner. Our volume-limited sample of ETGs is dominated by fast rotators (Paper II; Paper III), characterized by the presence of discs (Krajnović et al. 2013, hereafter Paper XVII) and closely linked to spiral galaxies (Cappellari et al. 2011b, hereafter Paper VII; Paper XX). Given the variety in the outer profiles of spiral galaxies (van der Kruit & Searle 1981; Pohlen & Trujillo 2006) it is unclear how profiles should be extrapolated. Using R_e and luminosities derived via extrapolation makes any derived trend necessarily assumption dependent. As we show in Section 4.4, the differences between different assumptions are quite significant. One can obtain different trends in scaling relations and reach different conclusions about their interpretation.

We argue that to make progress one should base conclusions on directly observable quantities. So for this work we define R_e as the radius containing half of the *observed* light, not half of the ill-defined amount of total light we think the galaxy may have. Of course even our approach does not solve the problem of determining an absolute normalization of R_e , and our sizes appear well reproducible only in a relative sense. The only real solution to the problem is to obtain deeper photometry so that R_e values converge and become essentially independent of the adopted profiles (Kormendy et al. 2009; Ferrarese et al. 2012). However, for massive galaxies in clusters, the distinction between galaxy light and intracluster light may become an issue. Earlier indications using deeper MegaCam photometry, which we have acquired for many of the galaxies in our sample (Duc et al. 2011, hereafter Paper IX), confirm that R_e determinations depend sensitively on the depth of the adopted photometry as expected.

If the x -axis is aligned with the galaxy photometric major axis, and the coordinates are centred on the galaxy nucleus, the surface brightness of an MGE model at the position (x', y') on the plane of the sky, already analytically deconvolved for the atmospheric seeing effects, can be written as (Emsellem et al. 1994)

$$\Sigma(x', y') = \sum_{j=1}^M \Sigma_j \exp \left[-\frac{1}{2\sigma_j^2} \left(x'^2 + \frac{y'^2}{q_j^2} \right) \right], \quad (9)$$

where M is the number of the adopted Gaussian components, having peak surface brightness Σ_j , observed axial ratio $0 \leq q'_k \leq 1$ and dispersion σ_k along the major axis. The total luminosity of the MGE model is then

$$L = \sum_{j=1}^M L_j = \sum_{j=1}^M 2\pi \Sigma_j \sigma_j^2 q'_j, \quad (10)$$

where L_j are the luminosities of the individual Gaussians.

In Cappellari et al. (2009), the effective radius of the MGE model was obtained by circularizing the individual Gaussians of the MGE, while keeping their peak surface brightness. This was achieved by

replacing (σ_j, q'_j) with $(\sigma \sqrt{q'_j}, 1)$. The luminosity of the circularized MGE enclosed within a cylinder of projected radius R is then

$$L(R) = \sum_{j=1}^M L_j \left[1 - \exp \left(-\frac{R^2}{2\sigma_j^2 q'_j} \right) \right]. \quad (11)$$

The circularized effective (half-light) radius R_e was found by solving $L(R) = L/2$, using a quick interpolation over a grid of $\log R$ values. When the MGE has constant axial ratio $q'_j = q'$ for all Gaussians, this approach finds the circularized radius $R_e = \sqrt{ab} = a\sqrt{q'}$ of the elliptical isophote containing half of the analytic MGE light, where a is the major axis of the isophote. This is the quantity almost universally used for studies of scaling relations of ETGs. When the axial ratios of the different Gaussians are not all equal, the approach finds an excellent approximation for the radius $R_e = \sqrt{A_e/\pi}$ of a circle having the same area A_e as the isophote containing half of the MGE light. In fact, we verified that for all the MGE of the ATLAS^{3D} sample, the two determinations agree with an rms scatter of just 0.17 per cent and only for four of the flattest galaxies the difference is larger than 3 per cent.

Hopkins et al. (2010) pointed out the usefulness of adopting as size parameter the major axis R_e^{maj} of the half-light isophote instead of the circularized radius R_e , when analysing results of simulations. The motivation is that R_e^{maj} is more physically robust and less dependent on inclination. Here, we also calculate R_e^{maj} for our observed galaxies as follows:

- (i) we construct a synthetic galaxy image from the MGE using equation (9), with size $\max(\sigma_j) \times \max(\sigma_j)$ (only one quadrant is needed for symmetry);
- (ii) we sample a grid of surface-brightness values $\mu_k = \mu(x_k, 0)$ along the MGE major axis, and for each value we calculate the light enclosed within the corresponding isophote;
- (iii) we find the surface brightness μ_e of the isophote containing half of the analytic MGE total light by solving $L(\mu) = L/2$ using linear interpolation;
- (iv) R_e^{maj} is the maximum radius enclosed inside the isophote μ_e (the largest x -coordinate).

We also calculate the circularized effective radius of the isophote $R_e = \sqrt{A/\pi}$ of area A and the effective ellipticity ε_e of the MGE model inside that isophote as (Cappellari et al. 2007)

$$(1 - \varepsilon_e)^2 = q_e'^2 = \frac{\langle y^2 \rangle}{\langle x^2 \rangle} = \frac{\sum_{k=1}^P F_k y_k^2}{\sum_{k=1}^P F_k x_k^2}, \quad (12)$$

where F_k is the flux inside the k th image pixel, with coordinates (x_k, y_k) and the summation extends to the pixels inside the isophote. A similar quantity was calculated from the original galaxy images in Paper III, but we use here this new determination for maximum consistency between our ε_e and the ellipticity of the MGE models in the tests of Fig. 4.

We studied the dependence on inclination of the two definitions of effective radii using the photometry of real galaxies. For this, we selected the 26 flattest galaxies in our sample, all having axial ratio $q' < 0.4$. These galaxies are likely to be close to edge-on. We assume that they are exactly edge-on and we then use the MGE formalism (equations 9, 13 and 14) to deproject the surface brightness and calculate the intrinsic luminosity density. We then project it back on the sky plane at different inclinations, from edge-on ($i = 90^\circ$) to face-on ($i = 0^\circ$). At every inclination, we calculate the two effective radii R_e and R_e^{maj} (Fig. 5). The comparison shows that, as expected, the R_e of flattened objects can be much smaller when objects are edge-on

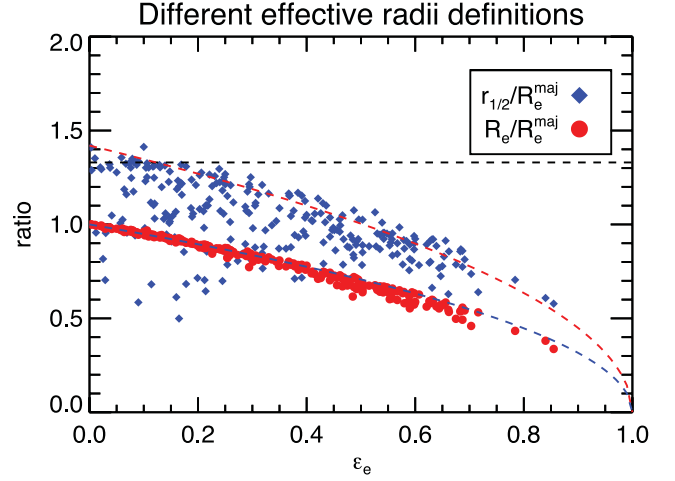


Figure 4. Different definitions of R_e as a function of the galaxy ellipticity. The red filled circles represent the projected radii R_e of a cylinder with the same area of the half-light isophote. The blue filled diamonds indicate the radii $r_{1/2}$ of a sphere with the same volume as the half-light isosurface. In both cases, the radii are normalized to R_e^{maj} , which is the projected semimajor axis of the half-light isophote, having ellipse of inertia of ellipticity ε_e . The red and blue dashed lines represent the relations $f(\varepsilon_e) = 1.42\sqrt{\varepsilon_e}$ and $f(\varepsilon_e) = \sqrt{\varepsilon_e}$, respectively. The horizontal dashed line marks the theoretical value $4/3$, which approximates the ratio $r_{1/2}/R_e$ for a number of simple theoretical profiles.

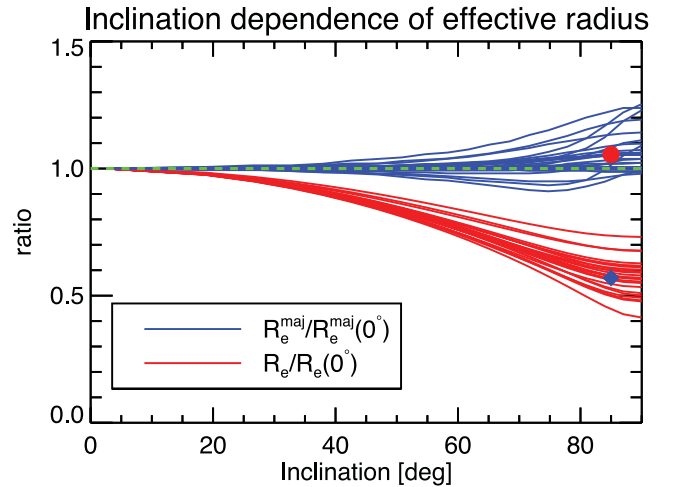


Figure 5. Inclination dependence for different definitions of the effective radius. The red lines show the change in the measured circularized R_e , normalized to the face-on value, when the inclination is changed from edge-on ($i = 90^\circ$) to face-on, for the 26 flattest ATLAS^{3D} galaxies. The blue diamond marks the median (43 per cent) of the maximum variation. The blue lines show the same variation with inclination of the major axis R_e^{maj} of the half-light isophote. The red circle represents the median (5 per cent) of the maximum variation.

than face-on, with a median decrease of 43 per cent (0.24 dex). The opposite is true for R_e^{maj} , but the variations are dramatically smaller, with a median increase of 5 per cent (0.02 dex). The two effective radii of course are the same for intrinsically spherical objects. The use of R_e^{maj} instead of R_e is especially useful when one considers that 86 per cent of the galaxies in ATLAS^{3D} (and in the nearby Universe) are disc like (Paper II, III and VII).

In what follows, we also need the radius $r_{1/2}$ of a sphere enclosing half of the galaxy light. For this, we need to derive the

intrinsic galaxy luminosity density from the MGE, assuming the best-fitting inclination of the JAM models. A possible deprojection of the observed MGE surface brightness can be derived analytically by deprojecting the individual Gaussians separately (Monnet, Bacon & Emsellem 1992). The solution is only unique when the galaxy is edge-on (Rybicki 1987). The deprojected luminosity density ν is given by

$$\nu(R, z) = \sum_{k=1}^M \frac{\Sigma_j q'_j}{\sqrt{2\pi} \sigma_j q_j} \exp \left[-\frac{1}{2\sigma_j^2} \left(R^2 + \frac{z^2}{q_j^2} \right) \right], \quad (13)$$

where the individual components have the same dispersion σ_j as in the projected case (9), and the intrinsic axial ratio of each Gaussian becomes

$$q_j = \frac{\sqrt{q_j'^2 - \cos^2 i}}{\sin i}, \quad (14)$$

where i is the galaxy inclination ($i = 90^\circ$ being edge-on). To calculate $r_{1/2}$ from the intrinsic density of equation (13) one can proceed analogously to the approach used to measure the circularized R_e . This is done by making the three-dimensional MGE distribution spherical, while keeping the same total luminosity and peak luminosity density of each Gaussian. This is achieved by replacing (σ_j, q_j) with $(\sigma_j q_j^{1/3}, 1)$. The light of this new spherical MGE enclosed within a sphere of radius r is given by

$$L(r) = \sum_{j=1}^M L_j [\text{erf}(h_j) - 2h_j \exp(-h_j^2)/\sqrt{\pi}], \quad (15)$$

with $h_j = r/(\sqrt{2} \sigma_j q_j^{1/3})$ and erf the error function. And the half-light spherical radius $r_{1/2}$ is obtained by solving $L(r) = L/2$ by interpolation. As in the projected case, when all Gaussians have the same $q_j = q$, which means that the density is stratified on similar oblate spheroids, the method gives the geometric radius $r_{1/2} = (abc)^{1/3} = a q^{1/3}$, where a is the semimajor axis of the spheroid. While when the q_j are different, this radius provides a very good approximation to the radius $r_{1/2} = [3V_e/(4\pi)]^{1/3}$ of a sphere that has the same volume V_e of the isosurface enclosing half of the total galaxy light.

In Fig. 4, we compare the three definitions of R_e as a function of the observed effective ellipticity ε_e of the MGE, for all the galaxies in the ATLAS^{3D} sample. Even though the galaxy isophotes are in most cases not well approximated by ellipses, and the galaxies are intrinsically not oblate spheroids, the ratio between R_e and R_e^{maj} follows the relation for elliptical isophotes. When the galaxies are very close to circular on the sky, R_e and R_e^{maj} agree by definition. The situation is very different regarding the relation between $r_{1/2}$ and R_e^{maj} . In this case, when the galaxy is edge-on, there is a simple ratio $r_{1/2}/R_e \approx 1.42$, but when the galaxies have lower inclinations, large variations in the ratio are possible, so that $r_{1/2}$ cannot be inferred from the observations, without the knowledge of the galaxy inclination, which generally require dynamical models. The situation is of course much simpler for spherical objects, in which case $r_{1/2}/R_e \approx 1.42$ as in the edge-on case. For comparison, Hernquist (1990) found the theoretical value $r_{1/2}/R_e \approx 1.33$ for his spherical models, while Ciotti (1991) has shown that for an $R^{1/m}$ model the ratio is confined between 1.34 and 1.36, when $m = 2-10$, and the same applies to other simple profiles (Wolf et al. 2010). As expected our ratio is slightly larger, given that our models, like real galaxies, do not extend to infinite radii.

3.3.2 Comparing effective and gravitational radius

For an isolated spherical system in steady state one obtains from the scalar virial theorem (Binney & Tremaine 2008)

$$M = \frac{r_g \langle v^2 \rangle_\infty}{G}, \quad (16)$$

where r_g is defined as the gravitational radius, which depends on the total and luminous mass distribution, M is the galaxy total luminous plus dark mass and $\langle v^2 \rangle_\infty$ is the mean-square speed of the galaxy stars, integrated over the full extent of the galaxy. In the spherical case $\langle v^2 \rangle_\infty = 3\langle \sigma_{\text{los}}^2 \rangle_\infty$ and

$$M = 3 \frac{r_g \langle \sigma_{\text{los}}^2 \rangle_\infty}{G}. \quad (17)$$

This formula is *rigorously* independent of anisotropy and only depends on the radial profiles of luminous and dark matter (Binney & Tremaine 2008, section 4.8.3).

When the spherical system is self-consistent [$L(r) \propto M(r)$] the gravitational radius can be easily calculated as

$$r_g = \frac{2L^2}{\int_0^\infty [L(r)/r]^2 dr}. \quad (18)$$

Here, we evaluate this expression using a single numerical quadrature via equation (15), from the same spherical deprojected MGE we used in the previous Section to calculate $r_{1/2}$. The MGE is obtained by deprojecting the observed surface brightness at the JAM inclination and subsequently making the MGE spherical while keeping the same peak stellar density and luminosity of every Gaussian. In this way, our calculation of r_g is rigorously accurate when the MGE is already spherical, while the formula provides a good approximation for flattened galaxies.

In Fig. 6, we plot the ratio $r_{1/2}/r_g$, for the full ATLAS^{3D} sample as a function of the non-parametric Third Galaxy Concentration (TGC) defined in Trujillo, Graham & Caon (2001) as the ratio between the light $L(R_e) = L/2$ enclosed within an isophote of radius R_e and the one $L(R_e/3)$ enclosed within an isophote with radius $R_e/3$. Graham, Trujillo & Caon (2001) have shown that this

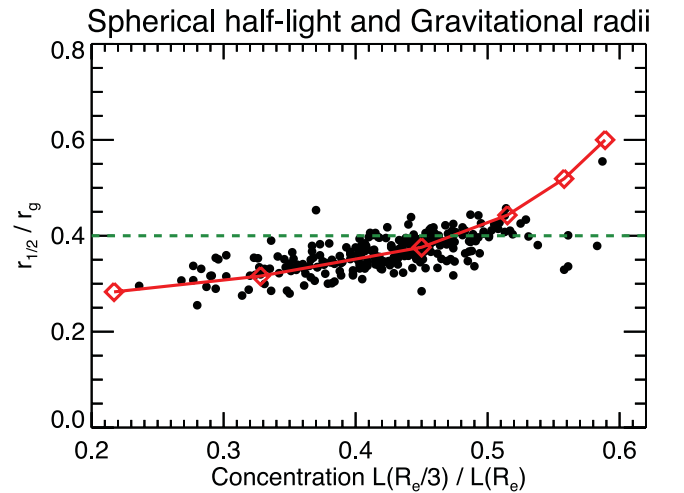


Figure 6. The black filled circles mark the ratio $r_{1/2}/r_g$ between the radius of the half-light sphere and the gravitational radius for all the galaxies in the sample. For comparison, the solid red line indicates the same ratio for a spherical galaxy with an $R^{1/m}$ surface brightness profile. From left to right, the red diamonds mark the locations $m = 1, 2, 4, 6, 8, 10$, respectively. The green dashed horizontal line indicates the theoretical value for a Hernquist (1990) profile.

choice leads to a more robust measure of concentration than popular alternatives (e.g. Doi, Fukugita & Okamura 1993). We compute the TGC from the circularized MGE using equation (11), as done for R_e . We find a trend in the ratio for the galaxies in our sample that varies between $r_{1/2}/r_g \approx 0.3$ and 0.4 for the range of galaxy concentrations we observed. For comparison, we also calculate the TGC and the corresponding r_g for spherical models described by the $R^{1/m}$ profile (Sérsic 1968). This was done by constructing analytic profiles, truncating them to $R < 4R_e$, to mimic the depth of the SDSS photometry, before fitting them with the one-dimensional MGE-fitting procedure of Cappellari (2002). Both TGC and $r_{1/2}/r_g$ span the ranges predicted for profiles with $m = 2-6$. Our trend in the ratio is more significant than the generally assumed near constancy around 0.40 ± 0.02 , first reported by Spitzer (1969) for different polytropes, which agrees with the theoretical value $r_{1/2}/r_g = (1 + \sqrt{2})/6 \approx 0.402$ for a Hernquist (1990) profile (Mamon 2000; Łokas & Mamon 2001). However, the variation is indeed rather small, being only at the ± 15 per cent level around a median value of 0.35 in our sample.

The relatively small variations of the ratio between the gravitational and intrinsic $r_{1/2}$ or projected R_e half-light radii, explain the usefulness of the latter two parameters in measuring dynamical scaling relations of galaxies. This fact, combined with the rigorous independence from anisotropy, also explains the robustness of a mass estimator like

$$M_{1/2} = k \frac{r_{1/2} \langle \sigma_{\text{los}}^2 \rangle_\infty}{G}, \quad (19)$$

when the stellar systems can be assumed to be spherical and kinematics is available over the *entire extent* of the system, as pointed out by Wolf et al. (2010). Assuming the measured ratio $r_{1/2}/r_g \approx 0.4$ for galaxies with the approximate concentration of an $R^{1/4}$ profile, already in the self-consistent limit the expected coefficient is $k \approx 3/0.4/2 = 3.75$, which is close, but 25 per cent larger than the corresponding coefficient $k = 3$ proposed by Wolf et al. (2010). However, the ratio $r_{1/2}/r_g$ we empirically measured on real galaxies does not assume that the outermost galaxy profiles are known and can be extrapolated to infinity, so it weakly depends on the depth of the photometry. For example, for a spherical galaxy that follows the $R^{1/4}$ profile to infinity, we obtain $r_{1/2}/r_g = 0.456$, which would imply $k = 3.29$ in the self-consistent limit. The remaining 10 per cent difference from Wolf et al. (2010) is easily explained by the small increase of $\langle \sigma_{\text{los}}^2 \rangle_\infty$ due to the inclusion of a dark halo.

3.3.3 Determination of σ_e

Unfortunately the quantities $\langle v_{\text{los}}^2 \rangle_\infty$, or $\langle \sigma_{\text{los}}^2 \rangle_\infty$ are currently only observable via discrete tracers in objects like nearby dwarf spheroidal galaxies (e.g. Walker et al. 2007), but it is still not a directly observable quantity in ETGs. Nonetheless, Cappellari et al. (2006) showed that in practice $\langle v_{\text{los}}^2 \rangle_e$, as approximated by σ_e^2 , which can be empirically measured for large samples of galaxies, can still be used to derive robust central masses when applied to real, non-spherical ETGs, with kinematics extended to about $1R_e$:

$$(M/L)(r = R_e) \approx 5.0 \times \frac{R_e \sigma_e^2}{GL}, \quad (20)$$

where $(M/L)(r = R_e)$ is estimated inside an isosurface of volume $V = 4\pi R_e^3/3$ (a sphere of radius R_e if the galaxy is spherical), and σ_e is the velocity dispersion calculated within a projected circular aperture of radius R_e . In this paper, we improve on the previous approach by measuring σ_e inside an effective ellipse instead of a circle.

The ellipse has area $A = \pi R_e^2$ and ellipticity ε_e . The measurement is done by co-adding the luminosity-weighted spectra inside the elliptical aperture and measuring the σ of that effective spectrum using PPXF (Cappellari & Emsellem 2004) and assuming a Gaussian LOSVD (keyword MOMENTS=2). Due to the co-addition, the resulting spectrum has extremely high S/N (often above 300) and this makes the measurement robust and accurate. When the SAURON data do not fully cover R_e , we correct the σ_e to $1R_e$ using equation 1 of Cappellari et al. (2006). σ_e has the big advantage over $\langle v_{\text{los}}^2 \rangle_e$ that it can also be much more easily measured at high redshift, as it does not require spatially resolved kinematics. Integrated stellar velocity dispersions have started to become measurable up to redshift $z \approx 2$ (Cappellari et al. 2009; Cenarro & Trujillo 2009; van Dokkum, Kriek & Franx 2009; Onodera et al. 2010; van de Sande et al. 2011). Moreover, the advantage of σ_e over the traditional central dispersion σ_c , is that it is empirically closer to the true second velocity moment $\langle v_{\text{los}}^2 \rangle_\infty$ that appears in the virial equation (17) and is directly proportional to mass. Making the good approximation $(M/L)(r = R_e) \approx (M/L)(r = r_{1/2})$, where $r_{1/2} \approx 1.33R_e$, one can rewrite equation (20) in a form that is directly comparable to equation (19)

$$M_{1/2} \approx 2.5 \times \frac{R_e \sigma_e^2}{G} \approx 1.9 \times \frac{r_{1/2} \sigma_e^2}{G}. \quad (21)$$

Note that the empirical coefficient 1.9 is significantly smaller than the value around 3.0 one predicts when using $\langle \sigma_{\text{los}}^2 \rangle_\infty$ in equation (19) and we will come back to this point in Section 4.4.

4 RESULTS

4.1 Uncertainty in the scaling relations parameters

4.1.1 Errors in L , R_e and σ

In the study of galaxy scaling relations, formal errors on L , R_e and σ are often adopted, as given in output by the software used for their extraction. These errors assume the uncertainties are of statistical nature. However, in many realistic situations the systematic errors are significant, but difficult to estimate. In this work, the availability of a significant sample of objects, with similar quantities measured via independent data or methods, allows for a direct comparison of quantities. This external comparison permits us to include systematic errors into our adopted errors, instead of just using formal or Monte Carlo errors.

In Paper XXI, we compare the total magnitude M_r of the MGE model, as derived from the SDSS+INT r -band photometry to various other sources in the literature. We conclude that our total M_r are accurate at the 10 per cent level, in the relative sense. This is the error we adopted in what follows. This accuracy is comparable to other state-of-the-art photometric surveys.

A comparison between the circularized half-light radii R_e of Paper I and the circularized R_e from the r -band MGE is shown in Fig. 7. In this case, the rms scatter is of $\Delta = 0.058$ dex, which would imply errors of $\Delta/\sqrt{2} = 10$ per cent in the individual R_e . This is the error we adopt for our R_e determination. This must still be a firm upper limit to the errors, given that any relative variations, among galaxies, in the colour gradients in r and K_s will increase the scatter. Remarkably in this case our scatter between SDSS r -band and 2MASS K_s bands, for the entire sample, is as small as the best agreement (0.05 dex) reported by Chen et al. (2010, their fig. 8), when comparing their R_e determinations versus those of Janz & Lisker (2008), using the very same SDSS g -band photometry and

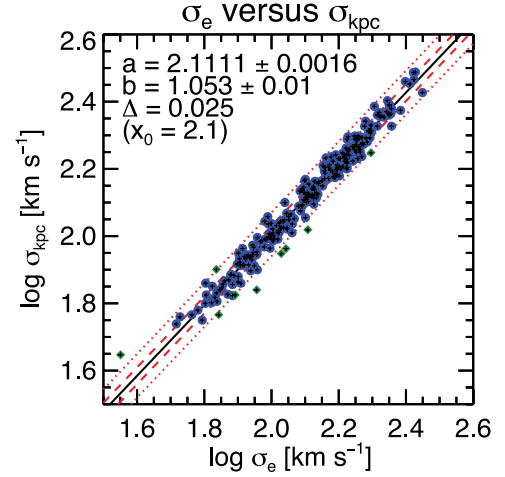
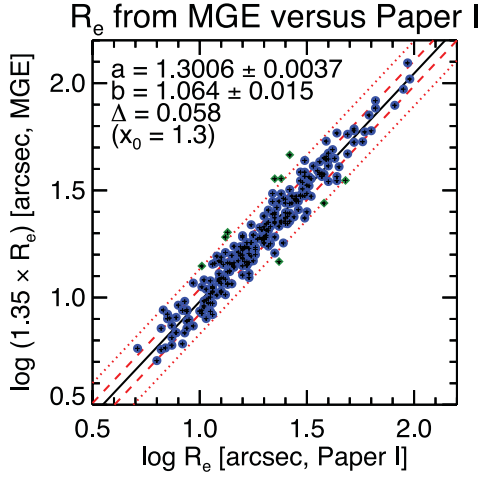


Figure 7. Testing the relative accuracy of size measurements. A comparison between the R_e from 2MASS plus RC3, matched to RC3 as described in Paper I, and the R_e from the MGEs. For a good match, the MGE values have been *increased* by a significant factor of 1.35. In what follows, the effective radii will always already include this multiplicative factor. The coefficients of the best-fitting relation $y = a + b(x - x_0)$ and the corresponding observed scatter Δ in y are shown at the top left of the plot. The two red dashed and dotted lines mark the 1σ bands (enclosing 68 per cent of the values for a Gaussian distribution) and 2.6σ (99 per cent), respectively. The outliers automatically excluded from the fit by the `LTS_LINEFIT` procedure are shown as green diamonds.

curve-of-growth technique. We are not aware of other published independent R_e determinations from different data that agree with such a small scatter, and for such a large sample. The rms scatter we measure is twice smaller than the Chen et al. (2010) comparison in the same band between SDSS and ACS Virgo Cluster Survey (ACSVCS). Our scatter is also twice smaller than a similar comparison we performed in Paper I between the R_e of 2MASS and RC3. We interpret the excellent reproducibility of our MGE R_e values, and the agreement with the values of Paper I, to the fact that in both 2MASS and our MGE models the total luminosities are *not* computed via an extrapolation of the profile to infinity, but simply measured from the data. This result is a reminder of the fact that extrapolation is a dangerous practice, which should be avoided whenever possible.

A very important feature of Fig. 7 is the significant offset by a factor of 1.35 between the MGE R_e and the values of Paper I, with the MGE values being smaller. In what follows, all our MGE effective radii will always already include this multiplicative factor. The values of Paper I were determined from a combination of 2MASS (Skrutskie et al. 2006) and RC3 (de Vaucouleurs et al. 1991) R_e measures. But they were scaled to match on average the values of the RC3 catalogue, which were determined using growth curves extrapolated to infinity. The RC3 normalization agree within 5 per cent with the SAURON determinations in Cappellari et al. (2006), Kuntschner et al. (2006) and Falcón-Barroso et al. (2011). Part of the 1.35 offset is simply due to the extrapolated light in an $r^{1/4}$ profile, outside the region where our galaxy extend on the SDSS or INT images. But the source of the remaining offset is unclear and confirms the difficulty of determining R_e . For comparison, in Paper I we showed that the 2MASS and RC3 values correlate well, but have an even more significant offset of a factor of 1.7!

Various comparisons of the accuracy of kinematic quantities have been performed in the literature (e.g. Emsellem et al. 2004). The general finding is that the measurements of the galaxies velocity dis-

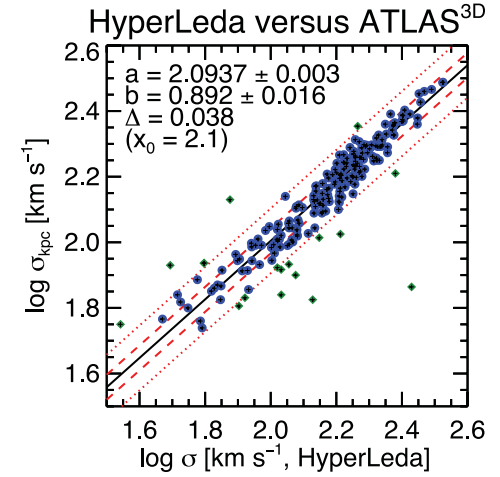


Figure 8. Testing the relative accuracy of σ_e determinations. Top panels: same as in Fig. 7 for the comparison between the dispersion σ_e , as measured with `PPXF` from the spectrum inside an elliptical aperture of area $A = \pi R_e^2$, and the quantity σ_{kpc} measured on a spectrum extracted inside a fixed circular aperture of radius $R = 1$ kpc. Bottom panels: same as in the top panel, for the comparison between our σ_{kpc} and the central σ provided by the HyperLEDA data base.

persion can be reproduced at best with an accuracy of ≈ 5 per cent, mainly due to uncertainties in the stellar templates and various systematic effects that are difficult to control. Here in Fig. 8 we test the internal errors of our kinematic determination by comparing σ_e against the velocity dispersion σ_{kpc} measured within a circular aperture of radius $R = 1$ kpc (close to the radius $R = 0.87$ kpc adopted in Jorgensen, Franx & Kjaergaard 1995b). This aperture is always fully contained in the observed SAURON field of view. We measure an rms scatter of $\Delta = 0.025$ dex between the two quantities, which corresponds to a 1σ error of 4 per cent in each value. The two values do not measure the same quantity, as the two adopted apertures and fitted spectra are different, and for this reason both the actual velocity dispersion and the stellar population change in the two `PPXF` fits. For this reason, the observed scatter provides a firm upper limit to the true internal uncertainties in σ_e . However, in what follows, we still assume a conservative error of 5 per cent in σ_e and σ_{kpc} , to account for possible systematics. The same choice was made e.g. in Tremaine et al. (2002) and Cappellari et al. (2006). We further compared our σ_{kpc} values against the literature σ compilation in the HyperLEDA data base (Paturel et al. 2003), for 207 galaxies in common with our sample. A robust fit between the logarithm of

the two quantities eliminating outliers with `LTS_LINEFIT` gives an observed rms scatter of 9 per cent ($\Delta = 0.038$ dex), likely dominated by the heterogeneity of the HyperLEDA values, and no significant offset (1 per cent) in the overall normalization. Apart from placing a very firm upper limit to our errors, this provides an external estimate of the typical uncertainties in the HyperLEDA values.

4.1.2 Errors in mass or M/L

To obtain an estimate of our mass and M/L errors for the full sample, we proceed similarly to Cappellari et al. (2006), namely we compare mass determinations using two significantly different modelling approaches. In Section 3.1.2, we described the six modelling approaches that were presented in Cappellari et al. (2012) and we also use in this paper. For this test, we compare the self-consistent model (A) and the models (B) which include an NFW halo with mass as free parameter. For the model with NFW halo, we then compute the $(M/L)_e \equiv (M/L)(r = R_e)$ by numerically integrating the luminous and dark matter distribution of the models. The total M/L enclosed within an isosurface of volume $V = 4\pi R_e^3/3$ is defined as follows

$$(M/L)(r = R_e) \equiv \frac{L(R_e) \times (M/L)_{\text{stars}} + M_{\text{DM}}(R_e)}{L(R_e)}, \quad (22)$$

where M_{DM} is the mass in the dark halo. This quantity is compared with the $(M/L)_{\text{JAM}}$ of the self-consistent model in the top panel of Fig. 9. The agreement is excellent, with no offset or systematic trend, and an rms scatter $\Delta = 0.038$ dex, consistent with errors of $\Delta/\sqrt{2} = 6$ per cent in each quantity. This value is the same we estimated as modelling error in Cappellari et al. (2006) and confirms the original estimate of the random modelling uncertainties.

Importantly, this result clarifies a misconceptions regarding the use of self-consistent models to measure the M/L inside $r \approx R_e$ in galaxies. Self-consistent models, like the one used in Cappellari et al. (2006), do *not* underestimate the total M/L as it is sometimes stated (e.g. Dutton et al. 2011a, section 3.7). Even though the model with dark halo has a total galaxy mass typically an order of magnitude larger inside the virial radius, and has a dramatically different mass profile at large radii, the model still measures an unbiased *total* M/L within a sphere of radius $r \approx R_e$, corresponding to the projected extent of the kinematical data. The robustness in the recovery of the enclosed total mass, in the region constrained by the data, even in the presence of degeneracies in the halo profile, was already pointed out by Thomas et al. (2005) and is demonstrated here with a much larger sample.

Of course the self-consistent $(M/L)_{\text{JAM}}$ is larger than the purely stellar one $(M/L)_{\text{stars}}$ if dark matter is present, according to the relation

$$(M/L)_{\text{JAM}} \approx (M/L)(r = R_e) = \frac{(M/L)_{\text{stars}}}{1 - f_{\text{DM}}(r = R_e)}, \quad (23)$$

where the fraction of dark matter contained within an isodensity surface of mean radius R_e is defined as

$$f_{\text{DM}}(r = R_e) \equiv \frac{M_{\text{DM}}(R_e)}{L(R_e) \times (M/L)_{\text{stars}} + M_{\text{DM}}(R_e)}. \quad (24)$$

The difference between $(M/L)_{\text{JAM}}$ and the stellar M/L inferred from population models can then be used to give quantitative constraints on the dark matter content and the form of the IMF, as done in Cappellari et al. (2006). Moreover, the self-consistent models do not imply or require the dark mass to be negligible inside $r \approx R_e$ as sometimes stated (e.g. Thomas et al. 2011). Although a number of

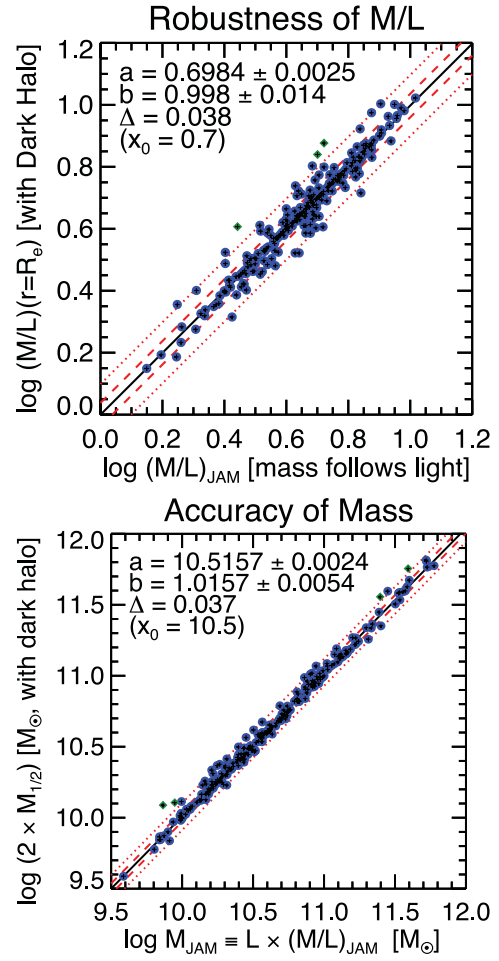


Figure 9. Accuracy of M/L and mass. Top panel: same as in Fig. 7 for the comparison between the $(M/L)_{\text{JAM}}$ of the best-fitting self-consistent (mass-follows-light) models, and the $(M/L)_e$, integrated within an isosurface of volume $V = 4\pi R_e^3/3$ (for a spherical galaxy a sphere of radius $r = R_e$), including the contribution of both the stellar and the dark matter component. There is no bias or systematic offset between the two determinations, which are consistent with an error of $\Delta/\sqrt{2} = 6$ per cent in each quantity. Bottom panel: same as the top panel for the comparison between the total mass of the self-consistent JAM model and twice the mass $M_{1/2}$ within the half-light isosurface, for the model with dark matter halo.

galaxies has non-negligible dark matter fraction, the total (luminous plus dark) M/L within $1R_e$ is still accurately recovered by the simple self-consistent models, without detectable bias. This makes the self-consistent models well suited to determine unbiased total M/L within $1R_e$ at high redshift (van der Marel & van Dokkum 2007; van der Wel & van der Marel 2008; Cappellari et al. 2009), where high-quality integral-field stellar kinematics still cannot be obtained and dark matter fractions cannot be extracted.

Using integral-field data the error in this measure of enclosed mass is as small as the one that can be obtained from strong lensing studies. The important difference between the two techniques is that the lensing results measure the total mass inside a projected cylinder (or elliptical cylinder), while the stellar kinematics gives the total mass inside a spherical (or spheroidal) region. The lensing mass should be larger than the dynamical one if dark matter is present in the galaxy. The difference between these two quantities provides a measure of the dark matter content along the LOS and

can be exploited to get some constraints on the dark matter profiles (Dutton et al. 2011b; Thomas et al. 2011).

In the bottom panel of Fig. 9, we compare the mass $M_{\text{JAM}} \equiv L \times (M/L)_{\text{JAM}}$, which we use extensively in this and in other papers of this ATLAS^{3D} series, with the total mass $M_{1/2}$ enclosed within an isosurface enclosing half of the total light, which is sometimes advocated to compare observations to galaxy simulations (e.g. Wolf et al. 2010). The plot illustrates the equivalence of the two quantities, for all practical purposes. It clarifies the physical meaning of M_{JAM} :

$$M_{\text{JAM}} \approx 2 \times M_{1/2}. \quad (25)$$

The JAM models with dark halo additionally provide an estimate of the dark matter fraction f_{DM} (equation 24) enclosed within the region constrained by the data $r = R_e$. For the galaxies where our kinematics does not cover $1R_e$, our f_{DM} will be more uncertain. The results is presented, as a function of galaxy stellar mass M_{stars} in Fig. 10 for the set of models (B), with an NFW halo, with mass as free parameter, and for the set of models (E), which have a cosmologically motivated NFW halo, uniquely specified by M_{stars} . We find a median dark matter fraction for the ATLAS^{3D} sample of $f_{\text{DM}} = 13$ per cent for the full sample and $f_{\text{DM}} = 9$ per cent for the best (qual > 1 in Table 1) models (B) and 17 per cent with models (E). These value are broadly consistent, but on the lower limit, with numerous previous stellar dynamics determinations inside $1R_e$ from much smaller samples and larger uncertainties: Gerhard et al. (2001) found $f_{\text{DM}} = 10$ –40 per cent from spherical dynamical modelling of 21 ETGs; Cappellari et al. (2006) inferred a median $f_{\text{DM}} \approx 30$ per cent by comparing dynamics and population masses of 25 ETGs, and assuming a universal IMF; Thomas et al. (2007b, 2011) measured $f_{\text{DM}} = 23 \pm 17$ per cent via axisymmetric dynamical models of 16 ETGs; Williams et al. (2009) measured a median fraction $f_{\text{DM}} = 15$ per cent with JAM models of 15 ETGs, as done here, but with more extended stellar kinematics to ≈ 2 – $3 R_e$. The results of Tortora et al. (2009) are not directly comparable, as they used spherical galaxy toy models and inhomogeneous literature data from various sources; however, they are interesting because they explored a sample of 335 ETGs, comparable to ours, and report a typical $f_{\text{DM}} = 30$ per cent by comparison with stellar population.

The quite small f_{DM} that we measure seems also consistent with the fact that the strong lensing analysis of the about 70 galaxies of the Sloan Lenses ACS sample Bolton et al. (2006) finds a logarithmic slopes for the *total* (luminous plus dark matter) density close to isothermal. Subsequent re-analyses of their data all confirmed a trend $\rho_{\text{tot}}(r) \propto r^{-2.0}$, with an intrinsic scatter of ≈ 0.2 (Koopmans et al. 2006, 2009; Auger et al. 2010b; Barnabè et al. 2011). In Fig. 2, we derive the same slope and intrinsic scatter for the stellar density alone, inside a sphere of radius $r = R_e$. This fact seems to suggest that dark matter does not play a significant role in galaxy centres and that the measured isothermal density slope is essentially due the stellar density distribution. Only a very steep dark matter slope close to isothermal $\rho_{\text{DM}}(r) \propto r^{-2.0}$ like the average stellar distribution could allow for significant dark matter fractions, while still being consistent with these observations. We are not aware of any theoretical or empirical evidence for these very steep dark matter cusps in galaxies.

4.2 The classic FP

Since the discovery of the FP relation between luminosity, size and velocity dispersion, in samples of local elliptical galaxies

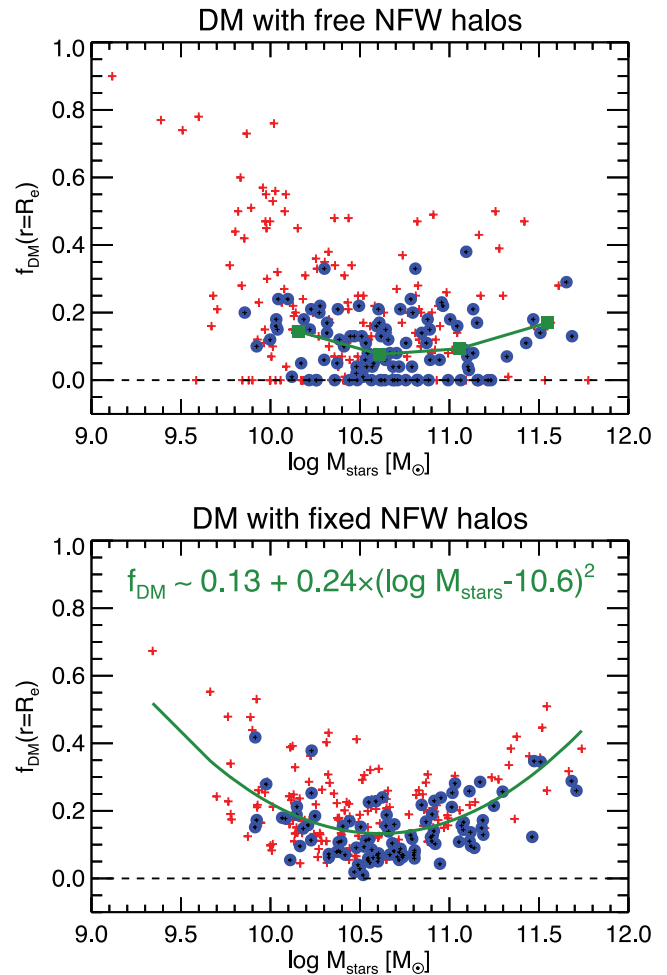


Figure 10. Dark matter fraction for ATLAS^{3D} galaxies. The open circles indicate the fraction f_{DM} of dark matter enclosed within the isosurface of volume $V = 4\pi R_e^3/3$ (in the spherical case within a sphere of radius R_e), for the best-fitting JAM models, as a function of the galaxy stellar mass M_{stars} inferred by the models. The blue filled circles are for the subset of 103 galaxies with the best models and data (qual > 1 in Table 1), while the red crosses indicate less good model fits or inferior data. The top panel corresponds to the results for models (B), with an NFW halo having mass as free parameter. The median is $f_{\text{DM}} = 13$ per cent for the full sample and $f_{\text{DM}} = 9$ per cent for the best models. In a number of cases, the model without dark matter is preferred. The solid green line indicates the mean for four mass bins. The bottom panel is the same as the top one, for the set of models (E) which has a cosmologically motivated NFW halo. The median $f_{\text{DM}} = 17$ per cent for all models. The green line represents a robust parabolic fit (written in the figure) to all the data. The robust result is that dark matter fractions are small, for halo slopes not steeper than NFW, $f_{\text{DM}} < 21$ per cent in 90 per cent of the best models.

(Djorgovski & Davis 1987; Dressler et al. 1987; Faber et al. 1987), numerous studies have been devoted to the determination of the FP parameters either including fainter galaxies (Nieto et al. 1990), fast rotating ones (Prugniel & Simien 1994) or lenticular galaxies (Jorgensen et al. 1996). The dependence of the FP parameters have been investigated as a function of the photometric band (Pahre et al. 1998; Scodreggio et al. 1998) or redshift (van Dokkum & Franx 1996). Moreover, galaxy samples of more than 10^4 galaxies have been studied (Bernardi et al. 2003; Graves, Faber & Schiavon 2009; Hyde & Bernardi 2009). In this section, before presenting our

result, we study the consistency of our FP parameters with previous studies.

Nearly all previous studies have used as variables the logarithm of the effective radius R_e , the effective surface brightness Σ_e and the (central) velocity dispersion σ . One of the reasons for this choice comes from the emphasis of the FP for distance determinations. Both Σ_e and σ are distance independent, so that all the distance dependence can be collected into the R_e coordinate by writing the FP as

$$\log R_e = a + b \log \sigma + c \log \Sigma_e. \quad (26)$$

In the top panel of Fig. 11, we present the edge-on view of our ATLAS^{3D} FP, obtained with the `LTS_PLANEFIT` routine, where we use as velocity dispersion σ_e (Section 3.3.3) as done in Cappellari et al. (2006) and Falc3n-Barroso et al. (2011), but here measured within an elliptical rather than circular isophote. Our best-fitting parameters $b = 1.063 \pm 0.041$ and $c = -0.765 \pm 0.023$ are formally quite accurate, but significantly different from what is generally found by other studies: the median of the 11 determinations listed in table 4 of Bernardi et al. (2003) is $b = 1.33$ and $c = -0.82$, with an rms scatter in the values of $\sigma_b = 0.12$ and $\sigma_c = 0.03$. The observed scatter we measure $\Delta \approx 0.091$ dex in $\log R_e$ is very close to what has been found by other studies (e.g. Jorgensen et al. 1996 find 0.084).

To understand the possible reason of this disagreement we test the sensitivity of our estimate to the sample selection and the size of the kinematical aperture used for the σ determinations. For this, we measure the velocity dispersion σ_{kpc} inside a circular aperture with radius $R = 1$ kpc (close to the radius $R = 0.87$ kpc adopted in the classic study by Jorgensen et al. 1995b). We also select the massive half of our sample by imposing a selection $\sigma_{\text{kpc}} > 130 \text{ km s}^{-1}$. The resulting FP is shown in the middle panel of Fig. 11, and now both the fitted values and the observed scatter agree with previous values. For comparison, we also show in the bottom panel of Fig. 11 the determination of the FP parameters, when using σ_e instead of σ_{kpc} , but keeping the same selection of the massive half of our ATLAS^{3D} sample $\sigma_e > 130 \text{ km s}^{-1}$. These values are also consistent with the literature. This illustrates the importance of sample-selection and σ extraction in the derivation of FP parameters. The increase of b as a function of the lower σ cut-off of the selection is fully consistent with the same finding by Gargiulo et al. (2009) and Hyde & Bernardi (2009) and we refer the reader to the latter paper for a more complete study of the possible biases in the FP parameters due to sample selection. The reason for the sensitivity of the FP parameters to the selection is a result of the fact that the FP is not a plane, but a warped surface, as we demonstrate in Paper XX by studying the variation of the $(M/L)_{\text{JAM}}$ on the Mass Plane (MP). So that the FP parameters depend on the region of the surface one includes in the fitting. This was also tentatively suggested by D’Onofrio et al. (2008).

Having shown that with our sample and method we can derive results that are consistent and at least as accurate as previous determinations, we now proceed to study the MP, by replacing the traditionally used stellar luminosity with the total dynamical mass. A similar study was performed by Bolton et al. (2007, 2008), and updated by Auger et al. (2010b), using masses derived from strong lensing analysis. They also call their plane the ‘Mass Plane’. Although our studies are closely related, one should keep in mind that, while the lensing masses are measured within a projected cylinder of radius $R = R_e/2$, parallel to the LOS, and for this reason they include a possible contribution of dark matter at large radii, our dynamical masses are measured within a sphere of radius $r = R_e$.

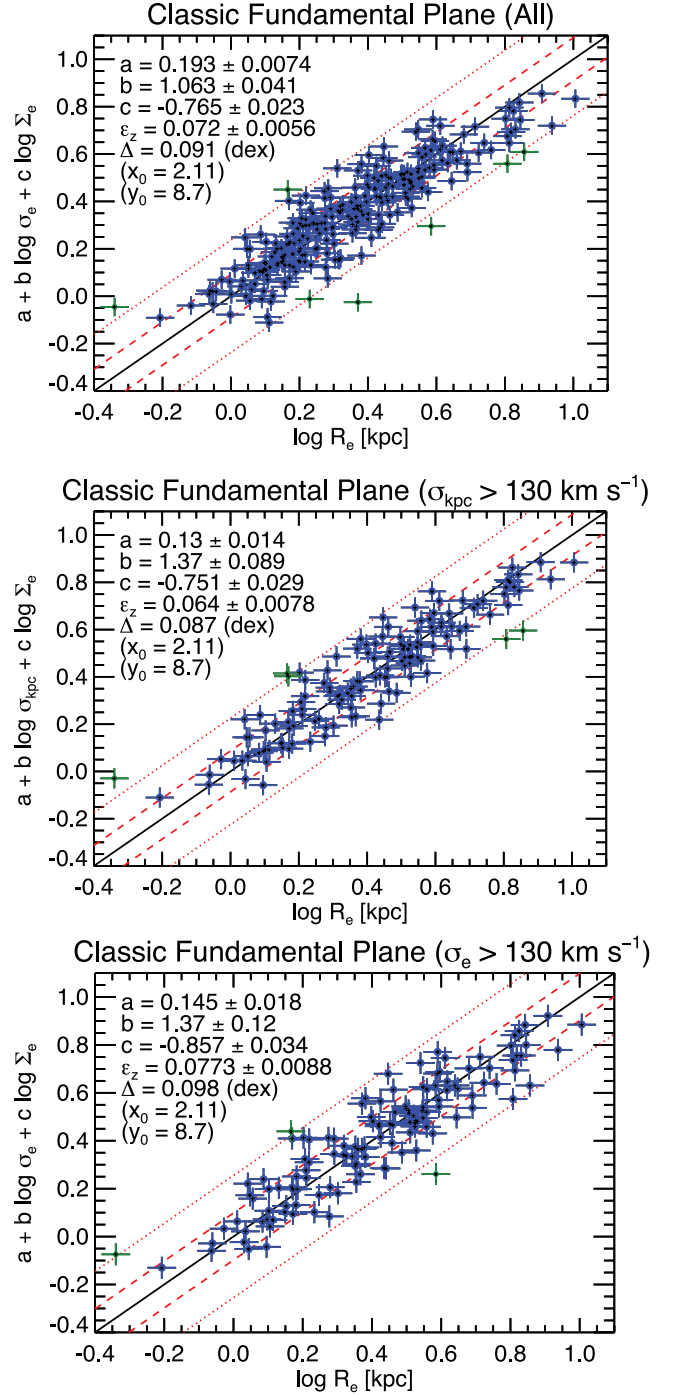


Figure 11. Classic FP. Top panel: edge-on view of the FP for all the ATLAS^{3D} galaxies. The coefficients of the best-fitting plane $z = a + b(x - x_0) + c(y - y_0)$ and the corresponding observed scatter Δ in z are shown at the top left of the plot. The two dashed lines mark the 1σ bands (enclosing 68 per cent of the values for a Gaussian distribution) and 2.6σ (99 per cent). The outliers excluded from the fit by the `LTS_PLANEFIT` procedure are shown with green symbols. The errors are the projection of the observational errors, excluding intrinsic scatter. Middle panel: same as in the top panel, with σ_{kpc} measured within a circle of radius $R = 1$ kpc. Only galaxies with $\sigma_{\text{kpc}} > 130 \text{ km s}^{-1}$ are included. Bottom panel: same as in the top panel using σ_e , but only including galaxies with $\sigma_e > 130 \text{ km s}^{-1}$.

4.3 From the FP to the MP

The classic form for the FP is ideal when the FP is used to determine distances. However, a different form seems more suited to studies where the FP is mainly used as a mass or M/L estimator. For this, we rewrite the FP as

$$\log \left(\frac{L}{L_{\odot,r}} \right) = a + b \log \left(\frac{\sigma_e}{130 \text{ km s}^{-1}} \right) + c \log \left(\frac{R_e}{2 \text{ kpc}} \right). \quad (27)$$

Here, we normalized the σ_e and R_e values by the approximate median of the values for our sample, to reduce the covariance in the fitted parameters and the error in a . Using L instead of Σ_e has the advantage that it reduces the covariances between the pairs of observables (Σ_e , R_e). Here, in fact, as opposed to when $\Sigma_e \equiv L/(2\pi R_e^2)$ is used, there is no explicit dependence between the three axes, which become independently measured quantities. The new fit to the FP is shown in the top panel of Fig. 12. In agreement with all previous authors, the fitted parameters are very different from the values $b = 2$ and $c = 1$ expected in the case of the virial equation (20). The relation shows a negligible increase in the observed rms scatter, from $\Delta = 0.091$ dex (23 per cent) to $\Delta = 0.10$ dex (26 per cent). This may be due to the reduced covariances between the adopted quantities: the new scatter is now a better representation of the true scatter in the FP relation.

In the bottom panel of Fig. 12, we show for comparison the relation obtained by replacing the total galaxy luminosity with the dynamical mass

$$M_{\text{JAM}} \equiv L \times (M/L)_{\text{JAM}} \approx 2 \times M_{1/2} \approx M_{\text{stars}}, \quad (28)$$

where $(M/L)_{\text{JAM}}$ is the total (luminous plus dark) dynamical M/L obtained using self-consistent JAM models (A), L is the total galaxy luminosity and $M_{1/2}$ is the total mass within a sphere of radius $r_{1/2}$ enclosing half of the total galaxy light, where $r_{1/2} \approx 1.33 R_e$ (Hernquist 1990; Ciotti 1991; Wolf et al. 2010; Fig. 4). The correctness of the $M_{\text{JAM}} \approx 2M_{1/2}$ approximation is illustrated in the bottom panel of Fig. 9. While the $2M_{1/2} \approx M_{\text{stars}}$ approximation is due to the relatively small amount of dark matter enclosed within $r = r_{1/2}$ (Fig. 10). This is only approximately true, generally within 20 per cent, but much larger errors are generally made when determining stellar masses from stellar population models, due the assumption of a universal IMF, which was recently shown not to represent real galaxies (van Dokkum & Conroy 2010; Cappellari et al. 2012). None of our conclusions is affected by the last approximation, which only serves to allow for comparisons of our results to previous similar studies that use stellar mass as parameter.

Two features are obvious from the plot: (i) there is a dramatic reduction of the observed scatter from $\Delta = 0.10$ dex (26 per cent) to $\Delta = 0.062$ dex (15 per cent). This shows without doubt that a major part of the scatter in the FP is due to variations in the M/L, in agreement with independent results from strong lensing (Auger et al. 2010b); (ii) the b coefficient substantially increases and is now much closer to the virial value $b = 2$, while the c coefficient remains nearly unchanged. The coefficients become consistent with the virial ones when using the effective radius R_e^{maj} , which is insensitive to projection effects, instead of R_e . This confirms that much of the deviation of the FP from the virial predictions is due to a systematic variation in M/L along the FP, not to non-homology in the luminosity profiles or kinematics, also in agreement with previous dynamical (Cappellari et al. 2006) and strong lensing results (Bolton et al. 2008; Auger et al. 2010b).

Galaxies are seen at random orientations so that projection effects should affect the measured σ_e . Given that the velocity ellipsoid in

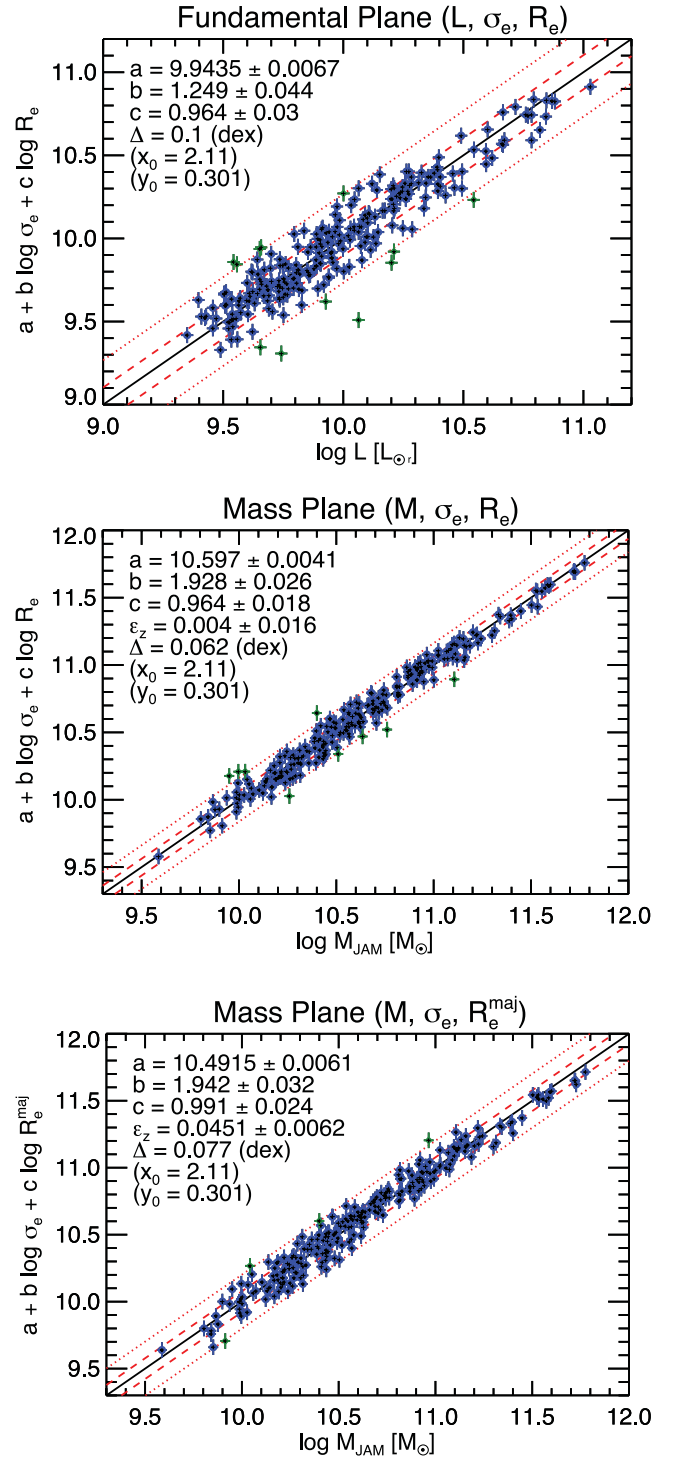


Figure 12. From the FP to the MP. Top panel: edge-on view of the FP. Symbols and lines are as in Fig. 11. Middle panel: edge-on view of the MP. Note the decrease in the scatter, when making the substitution $L \rightarrow M$, and the variation in the coefficients, starting to approach the virial ones $b = 2$ and $c = 1$. Bottom panel: same as in the middle panel, but using as effective radius the major axis R_e^{maj} of the effective isophote rather than the circularized radius. The scatter increases slightly, but the tilt is further decreased and now is consistent with the virial prediction.

ETGs is generally not too far from a sphere (Gerhard et al. 2001; Cappellari et al. 2007; Thomas et al. 2009), the velocity dispersion changes weakly with inclination, while the LOS velocity varies as $V = v \sin i$, where i is the galaxy inclination and v is the edge-on ($i = 90^\circ$) velocity. In this work, we have an estimate of the galaxy inclination for every galaxy in our sample, as measured via the JAM models. Although the inclination may not be always accurate, Cappellari (2008) showed that it agrees with the inclination inferred from dust discs, for a sample of four galaxies. Here, we extend the comparison to an additional sample of 22 galaxies with regular dust discs. The JAM inclination is found to always agree within the relative errors, with the inclination inferred from the dust discs, assumed to be circular and in equilibrium in the galaxies equatorial plane. Moreover, our tests using JAM to recover the inclination of N -body simulated galaxies also shows excellent agreement between the recovered values and the known ones (Paper XII). Our estimator of the ‘deprojected’ second velocity moment is then defined as

$$\langle v_{\text{rms}}^2 \rangle_e = \langle v^2 + \sigma^2 \rangle_e \equiv \frac{\sum_{k=1}^P F_k (V_k^2 / \sin^2 i + \sigma_k^2)}{\sum_{k=1}^P F_k}, \quad (29)$$

where i is the inclination of the best-fitting JAM models (A), V_k and σ_k are the stellar velocity and dispersion, extracted via PPXF adopting a Gaussian LOSVD, and F_k is the flux contained within that bin, for the P Voronoi bins (Cappellari & Copin 2003) falling within the ‘effective’ ellipse of major axis R_e^{maj} and ellipticity ε_e (Table 1). We found that $\langle v_{\text{rms}}^2 \rangle_e$ agrees with σ_e with an rms scatter of $\Delta = 0.025$ dex, consistent with our random errors. $\langle v_{\text{rms}}^2 \rangle_e$ did not improve any of our correlations with respect to the much simpler and robust σ_e , which also has the key advantage of not requiring spatially resolved integral field unit (IFU) kinematics. For this reason, we will not present any relation using $\langle v_{\text{rms}}^2 \rangle_e$.

The result of this exercise clearly shows that the existence of the FP is due to the fact that galaxies can be remarkably well approximated by virialized stellar systems with an M/L that varies systematically with their properties. These facts have been clearly realized since the discovery of the FP (Faber et al. 1987) and have been generally assumed in most recent studies (see Ciotti 2009 for a full discussion). The new findings on the tilt of the FP agree with a similar study of scaling relations in ETGs using accurate dynamical models and integral-field kinematics of a sample of just 25 galaxies (Cappellari et al. 2006) and with independent confirmations using strong gravitational lensing (Bolton et al. 2007, 2008; Auger et al. 2010b). Galaxy structural non-homology has a minor effect at best, when the determination of galaxy scaling parameters is pushed to the maximum accuracy and an attempt is made to remove the most important biases.

The level of accuracy at which the simple structural and dynamical homology approximation holds is not entirely expected, however, given the apparent complexity of galaxy photometry and kinematics. Of course the dynamical models assume equilibrium and rigorously satisfy the virial equations. One may think that a tight relation is a necessary feature of the approach. This is however not correct. It is true in fact that the models satisfy the scalar virial equation $2T + W = 0$ by construction, where T is the total kinetic energy and W is the total potential energy. However, given the complex multicomponent nature of galaxies, the presence of bars, the importance of projection and the fact that the potential energy should include dark matter, it is far from obvious that one should be able to define any simple empirical measure of projected radius on the galaxy, and a measure of velocity dispersion within a limited region, so that the virial equation can be written in the

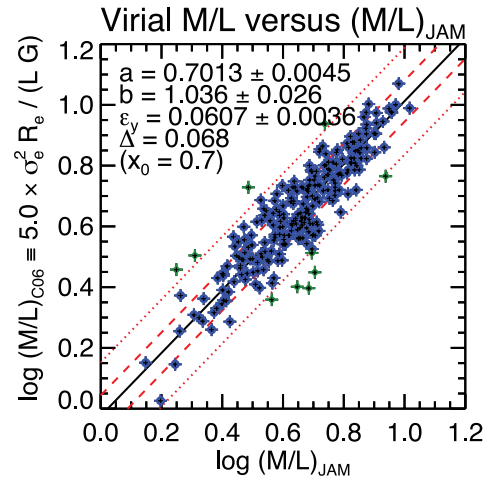


Figure 13. Accuracy of the simple virial estimate. A comparison between the virial estimator of Cappellari et al. (2006) and the more accurate JAM values. The inferred rms errors in the estimation of M/L are 15 per cent. Symbols and lines are as in Fig. 11.

simple form $M_{1/2} = k \sigma^2 R / G$ (designed for spherical homologous systems), with fixed exponents and nearly constant coefficient for the entire population!

4.4 Simple mass estimators

In Fig. 13, we present a direct comparison between the new $(M/L)_{\text{JAM}}$ estimates, which approximate the total M/L within an isosurface with volume $V = 4\pi R_e^3/3$, and the simple virial estimate of equation (20) taken from Cappellari et al. (2006). Considering the modelling errors of 6 per cent in M/L estimated in this paper, we infer an error of 15 per cent in the virial estimates. This shows that, although the virial estimates do not suffer from strong biases, they provide errors about a factor of 3 larger, even when using our good data.

Our finding does not seem to agree with the small systematic offsets recently reported by Thomas et al. (2011). The disagreement may be an effect of small sample statistics and larger errors, given that they studied only 16 objects and did not use integral-field data. However, even more likely is that the difference they find may be due to a systematic difference in their R_e determination, with respect to the SAURON ones. Our new empirical confirmation of the scaling of the coefficient in Cappellari et al. (2006), even in the presence of dark matter, also emphasizes the importance of using virial coefficients that are calibrated to the extent of the available kinematic data. The coefficient $k = 3.75$ given by Spitzer (1969) or $k = 3$ proposed by Wolf et al. (2010) for equation (19) should not be used to estimate central masses in ETGs, where stellar kinematics out to at most a couple of R_e is available and the corresponding value $k \approx 1.9$ of equation (21) applies. The difference of the two coefficients is due to the fact that, while the estimator of Wolf et al. (2010) is a theoretical one, designed for spherical geometry, very extended kinematics, and assumes galaxy profiles are known to infinite radii, the one by Cappellari et al. (2006) is an empirical one, designed for quantitative measures of masses in the central regions of ETGs. Both estimators are useful in their own range of applicability, but they should not be used interchangeably, unless one can tolerate systematic biases of ≈ 60 per cent in the absolute mass normalization.

In Fig. 14, we compare the ability of different simple mass estimators M_{vir} , all based on the scalar virial equation, to properly

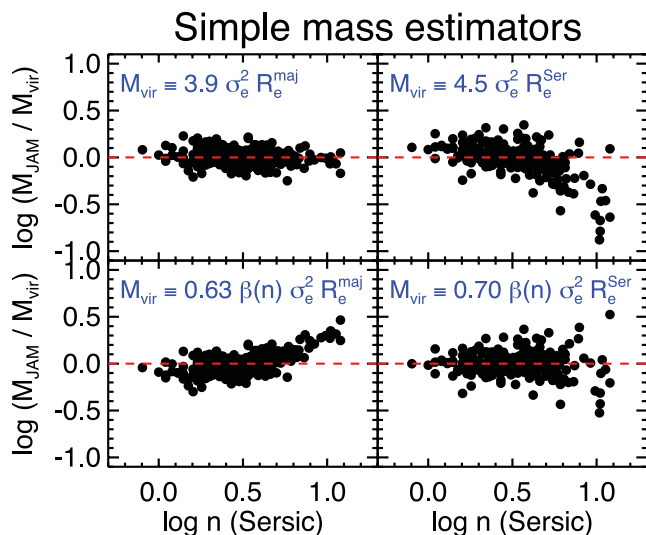


Figure 14. Comparing simple mass estimators. The ratio between the mass predicted by different estimators (written in blue in the panels), all based on the scalar virial equation, is compared to the rigorous determination using JAM models, and plotted as a function of the Sérsic index n from Paper XVII. The best estimator is the one in the top-left panel, which measures R_e from the data without extrapolation, and uses a fixed virial coefficient. When R_e is measured from a Sérsic fit to the profile extrapolated to infinite radii, the virial coefficient $\beta(n)$ needs to vary as a function of n , but the scatter in the recovered mass is large, especially for large n (bottom-right panel). Here, we used the theoretical prediction for $\beta(n)$ of equation (20) in Cappellari et al. (2006).

reproduce M_{JAM} . We show trends as a function of the Sérsic (1968) index n obtained for our galaxies by fitting a single Sérsic profile to the entire galaxy (for both E and S0 galaxies) and given in table C1 of Paper XVII. Our preferred estimator, which uses a fixed virial coefficient and the semimajor axis R_e^{maj} of the effective isophote, reproduces M_{JAM} better than any alternative one. It has no detectable trend with the Sérsic index and presents the smallest scatter (0.08 dex rms; top-left panel). The best-fitting coefficient of this estimator is smaller than the value 5.0 determined in Cappellari et al. (2006). This accounts for the fact that R_e^{maj} is systematically larger than the circularized radius R_e . In the bottom-left panel, we change the virial coefficient $\beta(n)$ according to the predictions of spherical isotropic models with a Sérsic profile (e.g. Prugniel & Simien 1997; Bertin et al. 2002). For this, we adopt the expression in equation (20) of Cappellari et al. (2006), which was calculated for σ_e measured in an aperture of radius R_e as adopted here. The plot shows a clear trend as a function of n , with a systematic bias of up to a factor of 3 for the largest n . This confirms that when R_e is measured without extrapolation of the data as done here, or in the ‘classic’ way (Burststein et al. 1987; Jorgensen et al. 1995a; Cappellari et al. 2006), using growth curves with fixed $n = 4$, a constant virial coefficient performs better than one that changes with n .

The opposite is true when R_e^{Ser} is the value obtained from Sérsic fits of the galaxy profile, assuming that the galaxy is described by that functional form out to infinite radii (from table C1 of Paper XVII). These R_e can be significantly different from the non-extrapolated values. Given that for both the R_e^{Ser} and R_e^{maj} determinations we used the very same images, the differences are entirely due to the *assumed* functional form of the surface brightness beyond the region where we have data. In this situation, adopting a fixed virial coefficient causes severe biases. The systematic bias in the virial estimator can be essentially removed adopting for $\beta(n)$ the

analytic prediction of Cappellari et al. (2006). However, the scatter in this estimator is significantly larger (0.13 dex rms) than the non-extrapolated one. Moreover, deviations are particularly large (up to a factor of 3) at the largest n , where a larger fraction of the total galaxy light is not actually observed on the images, but just extrapolated. Also note that an extra factor of 0.70 is needed in addition to the theoretically predicted coefficient $\beta(n)$. This factor must be calibrated empirically and makes the absolute normalization of the masses determined with this simple estimator rather uncertain.

These tests illustrate the extreme sensitivity of the reliability of masses estimated using the scalar virial equation on the technique adopted to measure R_e . They also show the difficulty of obtaining masses that are properly normalized. Ultimately the general unreliability and poor reproducibility of effective radii determined from photometry of different quality is the main limiting factor to a quantitative use of the scalar virial relations to measure accurate masses or M/L , when a proper absolute normalization is essential, like in IMF studies of distant galaxies (Cappellari et al. 2009). If different methods or extrapolations, applied to different, but high-quality photometric data of local galaxies, can produce revisions in R_e by as much as a factor of 2 (Kormendy et al. 2009; see also Chen et al. 2010), more significant biases should be expected when comparing local and high-redshift observations, as already pointed out by Mancini et al. (2010). When biases in R_e are present, only dynamical models can still provide robust central masses and M/L , due to the near insensitivity of the models to the shape of the outer mass and light profiles (van der Marel & van Dokkum 2007; van der Wel & van der Marel 2008; Cappellari et al. 2009).

4.5 The $(M/L)-\sigma_e$ relation

In the previous sections, we showed that the existence of the FP can be accurately explained by the virial relation combined with a smooth variation of the M/L . Here, we study the previously reported correlation $(M/L) \propto \sigma_e^{0.8}$ (in the I band) between the effective velocity dispersion and the dynamical M/L within a sphere of radius R_e (Cappellari et al. 2006; van der Marel & van Dokkum 2007). This relation was previously found to provide the tightest relation among other parameters of scaling relations (dynamical mass, luminosity or size), with an observed scatter of 18 percent and an inferred intrinsic one of just ~ 13 per cent, when using integral-field kinematics.

The $(M/L)-\sigma_e$ relation for the full ATLAS^{3D} sample is shown in the top-left panel of Fig. 15. Our new relation has an observed scatter of 29 percent, from which we infer an intrinsic scatter of 23 percent, when combining our 6 percent errors in the models with the distance errors for the various subsamples as described in section 2.2 of Paper I. We adopted as distance errors the median one for each given class of determinations reported in Paper I, instead of the individual errors, which are not easy to trust in every case, and that are likely dominated by systematics. The scatter is significantly larger than the previously reported one. The new relation has a formally accurate power slope of $b = 0.720 \pm 0.043$, which is a bit shallower than the previous one, based on a sample 10 times smaller than the current one.

To understand the reason for the differences between our $(M/L)-\sigma_e$ slope and previous determinations, in the top-right panel Fig. 15, we plot the $(M/L)-\sigma_e$ relation for the subset of 78 galaxies with SBF distances from Tonry et al. (2001), as done in both Cappellari et al. (2006) and van der Marel & van Dokkum (2007). The relation for this subset now steepens and becomes even steeper than the previous determinations. The reason for this is likely

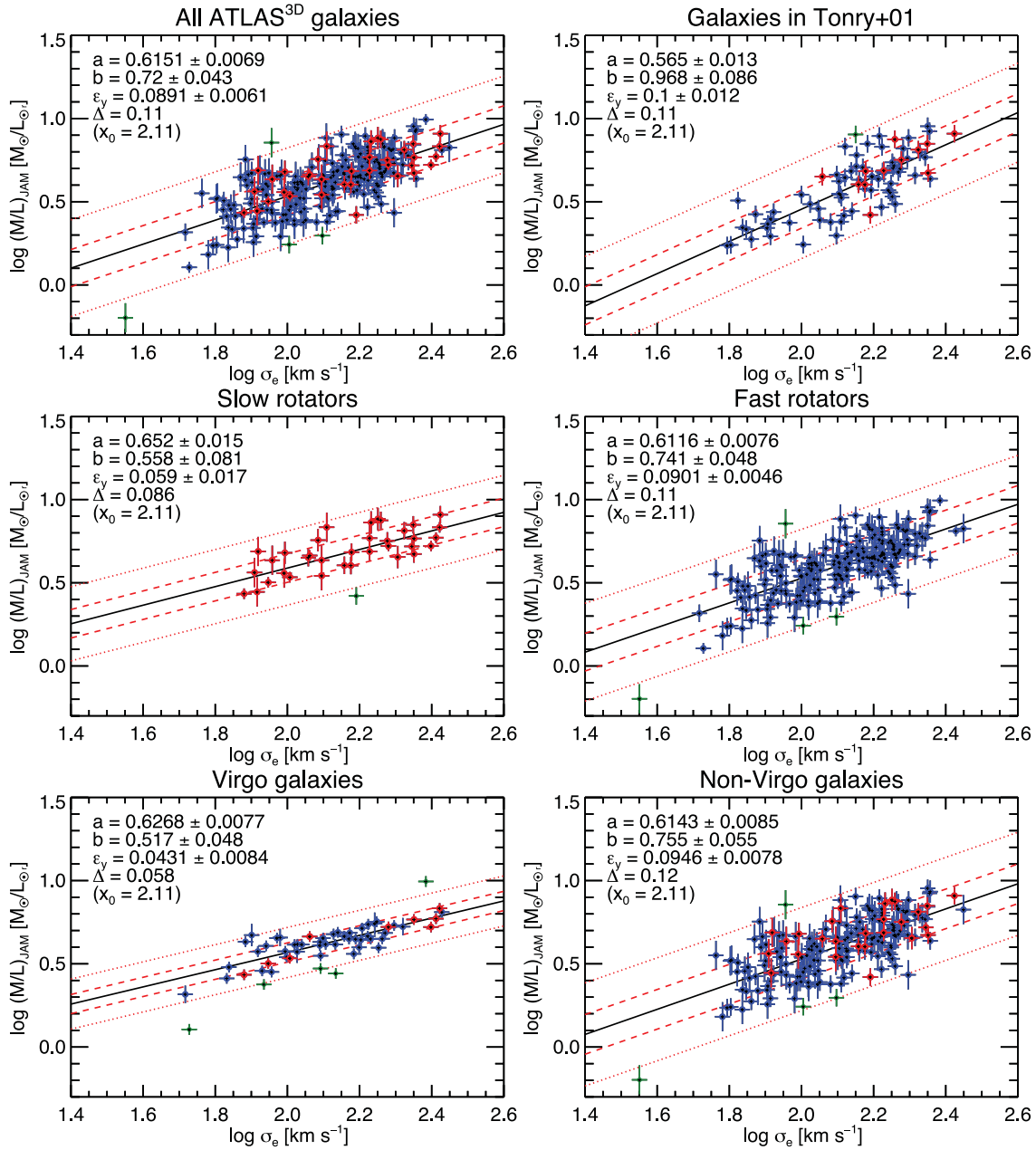


Figure 15. The $(M/L) - \sigma_e$ relation. From left to right and from top to bottom the relation is shown (i) for all ATLAS^{3D} galaxies, (ii) for the subset in Tonry et al. (2001), (iii) for the subset of slow rotators (from Paper III), (iv) for the subset of fast rotators, (v) for the subset of galaxies in the Virgo cluster (from Paper I) and (vi) for subset not in the Virgo cluster. In all plots the blue symbols represent fast rotators, while the red symbols slow rotators. The green symbols represent outliers excluded from the fit by `LTS_LINEFIT`.

related to the fact that the Tonry et al. (2001) subsample is biased towards elliptical galaxies, which tend to be the brightest in our sample. A change in slope is then expected from the curvature of the $(M/L) - \sigma_e$ relation, which is not clearly visible in our range of σ values, but is implied by the deviations from our relation when other classes of objects with smaller of larger σ are considered (Zaritsky, Gonzalez & Zabludoff 2006; Zaritsky, Zabludoff & Gonzalez 2008; Tollerud et al. 2011). A small but systematic increase in the slope is indeed visible when we select subsamples within different σ ranges from our ATLAS^{3D} sample. We conclude that the minor difference between our newly fitted value and the previous works is due to the difference in the sample selection. The present sample is not only much larger than the one used in previous studies, but also

volume limited so it provides a statistically representative view of the scaling relations in the nearby Universe.

In the middle panel of Fig. 15, we show the $(M/L) - \sigma_e$ of the 36 slow-rotator ETGs defined in Paper III and for the fast rotators. We confirm a detectable offset in the relation, with the slow rotators having slightly larger M/L than fast rotators, as previously reported in Cappellari et al. (2006). However, the difference is just at the 9 per cent level. There is also a change in the slope, with the slow rotators defining a more shallow relation than the full population. We also confirm the smaller scatter in the relation, as reported by Falcón-Barroso et al. (2011) for the colour- σ and FP relations. The slow rotators have an observed scatter of 22 per cent, and an inferred intrinsic one of 15 per cent in the $(M/L) - \sigma_e$ relation. This

is likely due to the fact that significant amounts of cold gas and star formation, which affect the M/L but not σ_e , are in fast rotators (Paper IV; McDermid et al., in preparation). The relation for the fast rotators (middle-right panel) agrees with the global one, as expected from the fact that they dominate the ATLAS^{3D} sample.

The dependence of the slope and zero-point of the $(M/L) - \sigma_e$ relation on environment effects is shown in the bottom panels of Fig. 15. As discussed in Paper VII, most of the environmental differences in the ATLAS^{3D} sample can be characterized by whether a galaxy belongs to the Virgo cluster or not. The left-hand panel shows the 58 ATLAS^{3D} galaxies in Virgo. They follow the same shallow relation as the slow rotators, but with the zero-point of the global relation. The observed scatter decreases to just 14 per cent, in part due to the accurate distances from ACSVCS (Mei et al. 2007). However, the intrinsic scatter $\varepsilon_{M/L}$ also further decreases to just 10 per cent. This is consistent with the intrinsic scatter measured by Cappellari et al. (2006), using a radically different set of models and different distance estimates (no ACSVCS), but on a sample that, contrary to the ATLAS^{3D} sample, was dominated by Virgo galaxies. The decrease in the scatter must be related to the decrease in the fraction of young objects in Virgo (Kuntschner et al. 2010; McDermid et al., in preparation). It again confirms that the scatter of the $(M/L) - \sigma_e$ relation is dominated by stellar population (including IMF) effects, as previously demonstrated for the FP. The two results are two ways of looking at the same thing, given that the $(M/L) - \sigma_e$ relation is the projection of the differences between the FP and MP along the σ_e axis. For completeness, we also show in the bottom right the relation for non-Virgo galaxies, which dominate the sample and again are consistent, albeit a bit steeper, than the global relation.

In the top panel of Fig. 16, we show how the tightness of the $(M/L) - \sigma_e$ relation can be used to cleanly select galaxies belonging to the Virgo cluster. Here, we selected all ATLAS^{3D} galaxies contained within a cylinder of radius of $R = 12^\circ$ centred on the Virgo cluster (approximately at the location of the galaxy M87) and assigned to all of them the cluster distance of $D = 16.5$ Mpc from Mei et al. (2007). We then used the `LTS_LINEFIT` routine to fit a line. Even in the presence of 20 dramatic outliers out of 79 objects, the method is able to robustly converge to a clean relation.⁴ The method selects 59 galaxies within the 99 per cent (2.6σ) confidence bands from the best-fitting relation. The plot reveals a tight sequence in the $(M/L) - \sigma_e$, which corresponds to galaxies in the Virgo cluster, with an observed scatter of $\Delta(M/L) = 0.071$ (18 per cent). It is reassuring to see that this relation, which uses no individual distance information for the galaxies, agrees both in the slope and zero-point with the ones for all ATLAS^{3D} galaxies, even though it has smaller scatter. Galaxies above the relation lie in the background of Virgo, and their difference in distance modulus from Virgo is 2.5 times the difference in $\log(M/L)$ from the best-fitting relations. In this fit, we assume that the distance error are due to the 1σ depth of the Virgo cluster. Adopting the value of $\sigma_D = 0.6 \pm 0.1$ from Mei et al. (2007), we derive an intrinsic scatter in M/L of $\varepsilon_{M/L} = 0.063$ dex (16 per cent).

When we select only the galaxies with surface brightness fluctuation (SBF) distances from the ACSVCS (Mei et al. 2007) (bottom panel of Fig. 16), we find a relation with the same slope, but a decreased observed scatter of $\Delta(M/L) = 0.047$ (11 per cent). For this relatively small, but still statistically significant sample of 32 galaxies, the inferred intrinsic scatter in M/L would be a mere 8 per cent!

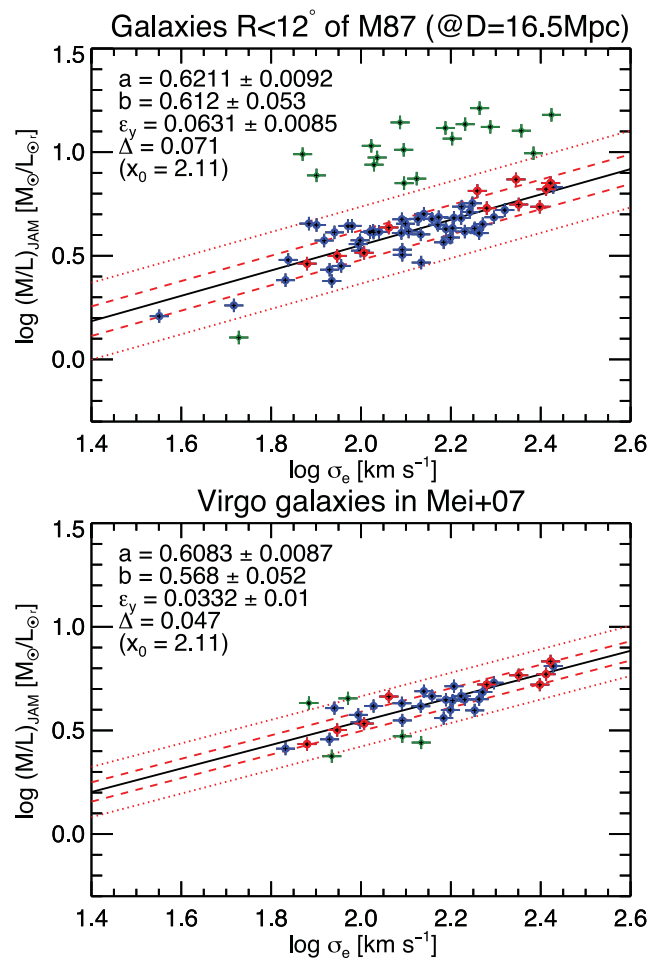


Figure 16. Scatter in the $(M/L) - \sigma_e$ relation in the Virgo galaxy cluster. Top panel: all ATLAS^{3D} galaxies within 12° of the centre of the Virgo cluster have been assigned a fixed distance of $D = 16.5$ Mpc. The measured M/L naturally defines a clean $(M/L) - \sigma_e$ relation for galaxies belonging to the cluster. The scatter in this relation is due to a combination of the cluster depth and the intrinsic scatter in M/L . Bottom panel: $(M/L) - \sigma_e$ relation for the galaxies in Mei et al. (2007). The accurate distances produce a quite significant decrease in the observed scatter, down to just 11 per cent, indicating that both the $(M/L)_{JAM}$ and the SBF distances are significantly more accurate than this value and confirming that the SBF distances are able to resolve the spatial structure of Virgo, along the LOS, as claimed.

Considering that ETGs appear to have very small fractions of dark matter in their central region (Fig. 10), a small scatter in dynamical M/L should be expected from the extreme tightness of the colour–magnitude relation in clusters (Bower, Lucey & Ellis 1992) and specifically for the ACSVCS galaxies (Chen et al. 2010), given that colour is a direct tracer of the M/L of the stellar population (Bell & de Jong 2001). Our small scatter finding confirms the remarkable accuracy of the ACSVCS SBF distances and their ability to resolve the cluster structure as claimed. It shows that the intrinsic $(M/L) - \sigma_e$ relation is extremely tight, but its study is limited in our sample by the distance errors. It would be valuable to perform a similar analysis as in the top panel of Fig. 16, with integral-field data and accurate models, in a cluster like Coma, sufficiently close that good stellar kinematics can be obtained, but sufficiently far that errors in the distance can be virtually ignored. The smaller intrinsic scatter inferred for this sample, with respect to the one in the top panel, suggests that, either they are not drawn from the same

⁴ Other robust methods like (i) minimizing the absolute deviation, (ii) using iterated biweight estimates or (iii) M-estimates (Press et al. 2007, section 15.7) failed to provide a sensible solution to this problem.

population, or the ACSVCS sample in Mei et al. (2007) spans a slightly smaller set of distances within the Virgo cluster than the ATLAS^{3D} Virgo sample. The tightness of this correlation also places stringent constraints on the possible intrinsic scatter on the IMF– σ trend that we discuss in Paper XX. Any IMF trend must satisfy the small scatter that we observe in this relation.

4.6 Relation between σ_e and the maximum circular velocity

Previous studies (Zaritsky et al. 2006, 2008; McGaugh et al. 2010; Dutton et al. 2011a) have tried to unify dynamical scaling relations of spiral galaxies and ETGs. For spirals, one can measure the rotation velocity of the gas, which appears in the Tully & Fisher (1977) relation between galaxy luminosity (or mass) and its maximum (asymptotic) circular velocity $\max(V_{\text{circ}})$, typically measured from the kinematics of the neutral gas at large radii. For ETGs, one can measure the velocity dispersion, which enters the Faber & Jackson (1976) and FP relations. Unification of the scaling relations is done by converting velocity dispersion into the circular velocity $V_{\text{circ}}(R_e^{\text{maj}})$ at the half-light radius or into the maximum one $\max(V_{\text{circ}})$ adopting constant factors.

Typical conversion factors for $V_{\text{circ}}(R_e^{\text{maj}})$ used in the literature range from $\sqrt{2}$ to $\sqrt{3}$ (Courteau et al. 2007). For example Padmanabhan et al. (2004) estimates $k \approx 1.65$. While Schulz, Mandelbaum & Padmanabhan (2010) adopts $k \approx 1.7$ and Dutton et al. (2011a) uses $k \approx 1.54$.

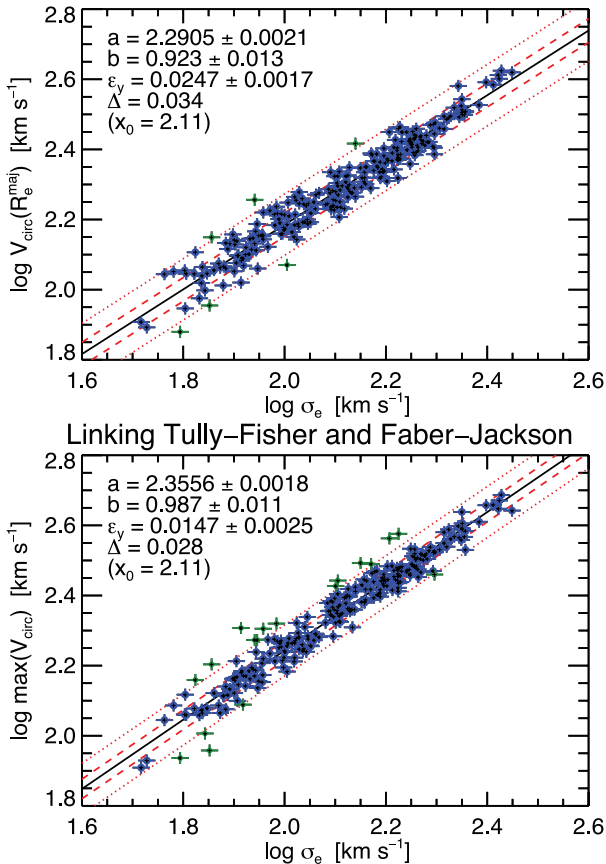


Figure 17. Circular velocity V_{circ} versus σ_e . Top panel: correlation between the circular velocity $V_{\text{circ}}(1R_e)$ inferred from our models at $1R_e$, and σ_e . Bottom panel: correlation between the peak circular velocity $\max(V_{\text{circ}})$ (within $1R_e$) and σ_e .

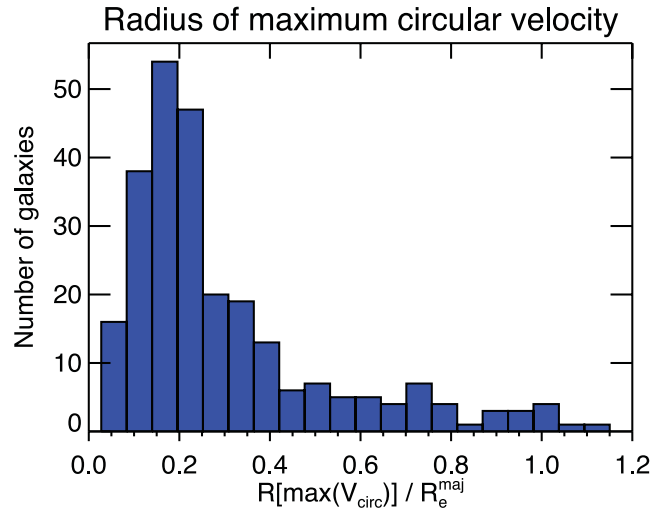


Figure 18. Histogram for the distribution of the radius R/R_e at which the maximum circular velocity $\max(V_{\text{circ}})$ is reached, as a fraction of the galaxy effective radius R_e .

Our data set provides accurate σ_e for all galaxies, together with circular velocities from our dynamical models. This allows for a robust empirical calibration of the relation. The correlation between σ_e and $V_{\text{circ}}(R_e^{\text{maj}})$ is shown in Fig. 17 and the best-fitting relation has the form

$$V_{\text{circ}}(R_e^{\text{maj}}) \approx 1.51 \times \sigma_e. \quad (30)$$

Considering the variety of photometric profile and galaxy flattening in our complete sample of ETGs, it is remarkable that the relation has a scatter of just 8 per cent, with a weak dependence on σ_e .

Even slightly tighter is the correlation between σ_e and $\max(V_{\text{circ}})$, which has the form

$$\max(V_{\text{circ}}) \approx 1.76 \times \sigma_e, \quad (31)$$

and an observed scatter of 7 per cent. Importantly, this coefficient shows essentially no variation with σ_e (the exponent is the one within the small errors). The $\max(V_{\text{circ}})$ defined here is the peak in the rotation curve within the region where we have stellar kinematics, which is generally within $1R_e$. As shown in Fig. 18, the inner maximum in the circular velocity $\max(V_{\text{circ}})$ is almost always reached well inside $1R_e$, with 85 per cent of the peaks happening at a radius smaller than $R_e/2$ and a median radius of just $R_e/5$. At these radii, the contribution of the stellar mass totally dominates the total mass. For this reason, $\max(V_{\text{circ}})$ should not be confused with the asymptotic value of the circular velocity at large radii, where dark matter dominates. The latter is generally used in the Tully & Fisher (1977) relation (but see Davis et al. 2011; hereafter Paper V). Although the so-called bulge–halo conspiracy (van Albada & Sancisi 1986) seems to generally make the two peak velocity values similar (e.g. see Williams et al. 2009), this fact has never robustly established for a significant sample of ETGs.

5 SUMMARY

We construct detailed dynamical models (JAM), based on the Jeans equations and allowing for orbital anisotropy, for the volume-limited and essentially mass-selected ATLAS^{3D} sample of ETGs. The models fit in detail the two-dimensional galaxy images and reproduce in detail the integral-field stellar kinematics obtained with SAURON out to about $1R_e$, the projected half-light radius. We derive accurate total mass-to-light ratios $(M/L)_e$ and dark matter fractions f_{DM} ,

within a sphere of radius $r = R_e$ centred on the galaxies. We infer masses $M_{\text{JAM}} \equiv L \times (M/L)_e \approx 2 \times M_{1/2}$, where $M_{1/2}$ is the mass within a sphere enclosing half of the galaxy light. We also measure stellar $(M/L)_{\text{stars}}$.

We test the accuracy of our mass determinations by running models with and without dark matter and we find that the enclosed total $(M/L)_e$ is a robust quantity, independent of the inclusion of a dark matter halo, with an rms accuracy of 6 per cent and negligible bias. In other words, even using simple mass-follow-light models, one recovers the total enclosed $(M/L)_e$ with good accuracy and small bias. We illustrate the techniques we use to measure radii and global kinematical quantities from our data, and to robustly fit linear relations or planes to the data, even in the presence of outliers and significant intrinsic scatter. We stress the difficulty of measuring absolutely calibrated effective radii R_e , and we argue against extrapolation in the profiles, for more reproducible results. Systematic offsets in R_e determinations are the main limitation for the use of the scalar virial relation for mass estimates, and may affect size comparisons as a function of redshift.

We find that the thin two-dimensional subset spanned by galaxies in the $(M_{\text{JAM}}, \sigma_e, R_e^{\text{maj}})$ coordinates system, which we call the MP has an observed rms scatter of 19 per cent, which would imply an intrinsic one of just 11 per cent. The MP satisfies the scalar virial relation $M_{\text{JAM}} \propto \sigma_e^2 R_e^{\text{maj}}$ within our tight errors. However, this is only true if one pays special attention to the methodology employed to determine the galaxy global parameters and in particular (i) one uses as scale radius the major axis R_e^{maj} of the ‘effective’ isophote enclosing half of the total projected galaxy light (without extrapolating the profile beyond the data), and (ii) one measures the velocity dispersion σ_e (which includes rotation and random motions) from a spectrum derived inside that effective isophote. This confirms with unprecedented accuracy previous claims (Cappellari et al. 2006; Bolton et al. 2008) that galaxies accurately satisfy the virial relations and that the existence of the FP is entirely explained by virial equilibrium plus a systematic variation in the total $(M/L)_e$.

We revisit the $(M/L)_e - \sigma$ relation and measure a marginally shallower observed slope than previously reported. The minor difference can be explained by selection of the sample of galaxies previously used to fit the relations. We find that the correlation depends both on galaxy rotation and environment, in the sense that both for the subsamples of the galaxies in Virgo, or for the subsample of slow rotators, the relation is more shallow and has a reduced scatter. In the best case, when the most accurate distances are used, the observed scatter drops to 11 per cent and the intrinsic one is estimated to be a mere 8 per cent.

We study the correlation between σ_e and the circular velocity from the dynamical models. We find that $V_{\text{circ}}(R_e^{\text{maj}}) \approx 1.51\sigma_e$ and $\max(V_{\text{circ}}) \approx 1.76\sigma_e$. The relations have an observed scatter of 7–8 per cent and the coefficient is independent of σ_e .

The accurate global dynamical scaling parameters for the ETGs in the ATLAS^{3D} sample are used in the companion Paper XX to explore different projection of the MP and the variation of galaxy physical parameters.

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SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

Table 1. Scaling relations and mass-follows-light JAM models parameters for the ATLAS^{3D} sample of 260 ETGs (<http://mnras.oxfordjournals.org/lookup/suppl/doi:10.1093/mnras/stt562/-/DC1>).

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